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# **Core Cosmology Library Documentation**

*Release 2.X*

**LSST DESC**

**Aug 07, 2020**



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The Core Cosmology Library (CCL) is a standardized library of routines to calculate basic observables used in cosmology. It will be the standard analysis package used by the LSST Dark Energy Science Collaboration (DESC).

The core functions of this package include:

- Background quantities (Hubble parameter  $H(z)$ , distances etc.).
- Linear growth factor  $D(z)$  and growth rate  $f(z)$ .
- Linear matter power spectra  $P(k)$  from Boltzmann codes (CLASS, CAMB) and approximate fitting functions.
- Non-linear matter power spectra using HaloFit and the Mira-Titan Emulator.
- Approximate baryonic modifications to the matter power spectra  $\Delta_{\text{baryons}}^2$
- Angular power spectra  $C_\ell$  and correlation functions  $\xi$  for arbitrary combinations of tracers including number counts, shear and CMB lensing, as well as custom-made tracers.
- A comprehensive halo model framework able to combine different prescription for the halo mass function  $dn/dM$ , halo bias  $b(M)$ , concentration-mass relation  $c(M)$ , mass definitions, and halo profiles, as well as to provide predictions for the halo-model power spectrum of arbitrary quantities.
- Support for  $\Lambda$  CDM, and  $w_0 - w_a$  CDM cosmologies with curvature, as well as simple modified gravity extensions ( $\Delta f(z)$  and  $\mu - \Sigma$ ).

The source code is available on github at <https://github.com/LSSTDESC/CCL>.



CCL can be installed from `pip`, `conda`, or directly from source. It is configured to install most of its requirements automatically. However, if you want to use CCL with Boltzmann codes like `CLASS` or `CAMB`, or do perturbation theory calculations with `FAST-PT`, you will need to make sure these packages and their Python wrappers are installed as well. See the instructions for *Getting a Boltzmann Code* and *Getting FAST-PT* below.

CCL works on Linux or Mac OS. Windows installation is not supported.

Once installed, you can take CCL for a spin by following the *Quickstart* instructions.

### 1.1 With conda

Installing CCL with `conda` will also install a copy of `pycamb`, the Python wrapper for `CAMB` in your environment.

```
$ conda install -c conda-forge pycc1
```

### 1.2 With pip

The PyPi installation will actually build a new copy of CCL from source as the code is installed. In order to do this, you will need `CMake` installed on your system. See the instructions below for *Getting CMake*.

Once you have `CMake`, simply run:

```
$ pip install pycc1
```

### 1.3 Getting a Boltzmann Code

In order to use CCL with a Boltzmann code, you will need the Python wrappers for either `CLASS` or `CAMB`.

### 1.3.1 CLASS

In order to use CCL with CLASS, you need to install the CLASS Python wrapper `classy`. See their instructions [here](#). Note that you may need to edit the `Makefile` in the CLASS repo to work with your system. Please report any installation issues to the CLASS developers on their [issues tracker](#).

### 1.3.2 CAMB

If you are working in a conda environment, then CAMB is available via

```
$ conda install -c conda-forge camb
```

An installation with `pip` should work as well. See the [CAMB](#) repo for more details. Note that if you installed CCL with `conda`, `camb` should already be in your environment.

### 1.3.3 ISITGR

In order to use CCL with ISITGR, you need to install the ISITGR Python wrapper `isitgr` with:

```
$ pip install isitgr [--user]
```

See further instructions [here](#).

If you are working in a conda environment, then ISITGR is also available via

```
$ conda install -c conda-forge isitgr
```

Note that if you installed CCL with `conda`, `isitgr` should already be in your environment.

## 1.4 Getting FAST-PT

To use FAST-PT with CCL, you can install it with:

```
$ pip install fast-pt
```

Note the hyphen in the package name! You can also get it directly from the [FAST-PT](#) repo.

## 1.5 Getting CMake

The `pip` installation of CCL requires that CMake is installed on your system. CMake is available from package managers like `apt-get` and `homebrew`. You need version 3.2 or higher.

### 1.5.1 Ubuntu

```
$ sudo apt-get install cmake
```



## 1.5.2 OS X

On MacOS X you can either install with a DMG from [this page](#) or with a package manager such as [homebrew](#), [MacPorts](#), or [Fink](#).

For instance with homebrew, you can run

```
$ brew install cmake
```

## 1.6 Known Installation Issues

1. For some Mac OSX versions, the standard C headers are not in the usual spot, resulting in an error of fatal error: 'stdio.h' file not found. This can be resolved with the command:

```
$ sudo installer -pkg /Library/Developer/CommandLineTools/Packages/macOS_SDK_
↳headers_for_macOS_10.14.pkg -target /
```

which will install all the required headers into `/usr/include`.

On Mac OSX 10.15 or greater, this patch is no longer included. Instead, you can manually add the location of required headers to your CPATH by running the following, or adding to your `.bash_profile`:

```
$ export CPATH="/Applications/Xcode.app/Contents/Developer/Platforms/MacOSX.
↳platform/Developer/SDKs/MacOSX.sdk/usr/include"
```

2. Newer versions of Xcode do not automatically have the required command line tools installed. This can be done from the command line:

```
$ sudo xcode-select --install
$ sudo xcodebuild -license
```

## 1.7 Uninstalling CCL

CCL can be uninstalled using the uninstallation functionality of the package manager (i.e., `conda` or `pip`) you used to install it. When in doubt, first try with `conda` and then try with `pip`. In either case, the command is

```
$ [conda|pip] uninstall pycc1
```



CCL is structured around *Cosmology* objects which hold the cosmological parameters and any tabulated data associated with a given cosmology. The library then provides functions to compute specific quantities of interest. See the full API documentation through the *pyccl* module and submodules for more details.

Further, CCL follows the following conventions:

- all units are non-h-inverse (e.g., Mpc as opposed to Mpc/h)
- the scale factor *a* is preferred over redshift *z* as a time coordinate.
- the *Cosmology* object always comes first in most function calls
- argument ordering for power spectra is (*k*, *a*)

This example computes the comoving distance and HALOFIT non-linear power spectrum using the BBKS transfer function:

```
>>> import pyccl
>>> cosmo = pyccl.Cosmology(Omega_c=0.25, Omega_b=0.05,
                           h=0.7, n_s=0.95, sigma8=0.8,
                           transfer_function='bbks')
>>> pyccl.sigma8(cosmo) # get sigma8
0.7999999999999998
>>> z = 1
>>> pyccl.comoving_radial_distance(cosmo, 1./(1+z)) # comoving distance to z=1 in Mpc
3303.5261651302458
>>> pyccl.nonlin_matter_power(cosmo, k=1, a=0.5) # HALOFIT P(k) at k,z = 1,1
143.6828250598087
```

See *Notation, Models and Other Cosmological Conventions* for more details on the supported models for various cosmological quantities (e.g., the power spectrum) and the specification of the cosmological parameters.

A comprehensive set of examples showcasing the different types of functionality implemented in CCL can be found [here](#).



This code has been released by DESC, although it is still under active development. It is accompanied by a journal paper that describes the development and validation of *CCL*, which you can find on the [arxiv](#). If you make use of the ideas or software here, please cite that paper and provide a link to the repository <https://github.com/LSSTDESC/CCL>. You are welcome to re-use the code, which is open source and available under terms consistent with our [LICENSE \(BSD 3-Clause\)](#).

External contributors and DESC members wishing to use *CCL* for non-DESC projects should consult with the TJP working group conveners, ideally before the work has started, but definitely before any publication or posting of the work to the arXiv.

For free use of the `CLASS` library, the `CLASS` developers require that the `CLASS` paper be cited, `CLASS II: Approximation schemes`, D. Blas, J. Lesgourgues, T. Tram, arXiv:1104.2933, JCAP 1107 (2011) 034. The `CLASS` repository can be found in <http://class-code.net>.

The `CAMB` developers have released `CAMB` under the `LGPL` license with a few additional restrictions. Please read their [LICENSE file](#) for more information.



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### Reporting Bugs / Contacting a Human

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If you have encountered a bug in CCL report it to the [Issues](#) page. This includes problems during installation, running the tests, or while using the package. If possible, provide an example script that reproduces the error.

If you find a discrepancy between a computed quantity from CCL and another source (or from also from CCL) please describe the quantity you are computing. If possible, provide an example script and a plot demonstrating the inconsistency.

Finally, if all else fails, you can contact the [administrators](#) directly.





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## Terms of Reference and Development Principles

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This document lays out terms of reference for CCL developers and contributors in the wider TJP and LSST DESC context.

### 5.1 Background

CCL was created to provide theoretical predictions of large-scale structure statistics for DESC cosmological analyses but it has also become a publicly available tool.

### 5.2 Scope

CCL has a commitment to support key DESC analyses. In this regard, CCL aims to

- support cosmological models that are priorities for WGs (e.g., as defined by the “Beyond  $\Lambda$ CDM” taskforce);
- ensure sufficient flexibility such that modifications can be implemented at a later stage as needed (e.g., models for observational systematics or changes to how the non-linear power spectrum is computed for various parts of the analysis);
- support core predictions (e.g., shear correlation functions), but not necessarily every statistic that could be computed from those core predictions (e.g., COSEBIs).

CCL interface support is as follows.

- Public APIs are maintained in Python only (i.e., version bumping is not necessary following changes in the C interface).
- The C implementation can be used for speed as needed.
- Documentation should be maintained in the main README, readthedocs and the benchmarks folder.
- Examples will be maintained in a separate repository.

Boundaries of CCL (with respect to various models and systematics)

- Not all models need to have equal support. CCL aims to support the DESC analyses, not to support all possible statistics in all models.
- CCL should provide a generic framework to enable modeling of systematics effects. However, overly specific models for systematics, for example, for galaxy bias, detector effects or intrinsic alignments, are best located in other repositories (e.g., firecrown).

Boundaries of CCL (with respect to other TJP software)

- TJP will necessarily develop other software tools to support DESC cosmological analyses. CCL development should ensure internal consistency between the various tools by defining a common parameterization of theoretical quantities (e.g., kernels for Limber integration, the metric potentials, etc.).
- CCL development should also proceed in a manner to avoid significant duplication of effort within the collaboration.

### 5.3 Standards to establish the quality of code that can be part of CCL

- Contributions to CCL should be well-documented in python (only doc-string level docs are required, readthedocs does the rest). C code is expected to be commented, though not documented.
- Features added to CCL should pass required tests.
  1. one (publicly available) benchmark with an independent prediction should be provided to test the specific feature that has been added. The benchmark code can use CCL input as long as that is not affecting the validation procedure.
  2. Tests should run in continuous integration scheme used for CCL.
  3. Unit tests should be written following the suggestions of the PR reviewers.
- All PRs are code reviewed by at least one person (two are suggested for PRs that bring in new features or propose significant changes to the CCL API).
- CCL uses semantic versioning.
- We should aim to tag new versions with bug fixes on a monthly basis with the expectation that no release is made if no new bugs have been fixed.
- Critical bug fixes should be released almost immediately via bump of the micro version and a new release.

### 5.4 Guidelines towards contribution

- Contributions should be made via PRs, and such PRs should be reviewed as described above.
- Response to code review requests should be prompt and happen within a few days of being requested on github by the author of the PR. Code review by members of the CCL development team should happen within a week of the request being accepted.
- The CCL *Developer Guide* should be consulted by those making PRs.
- Developers should use standard DESC channels to interact with the team (e.g., Slack, telecons, etc.).
- Developers should seek consensus with the team as needed about new features being incorporated (especially for API changes or additions). This process should happen via the CCL telecons, slack channel, or github comments generally before a new feature is merged. More minor changes, like bug fixes or refactoring, do not necessarily need this process.

- External contributions. They come in different forms: bug fixes or new features. They should proceed in full awareness of the LSST DESC Publication Policy. In particular, the use of new features added to the library, but not officially released, may require more formal steps to be taken within the DESC. External contributors and DESC members wishing to use CCL for non-DESC projects should consult with the TJP working group conveners, ideally before the work has started, but definitely before any publication or posting of the work to the arXiv.



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## API Changes and Stability

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CCL follows the conventions of [semantic versioning](#). Semantic versioning is a consistent set of rules for constructing CCL version numbers so that CCL users can understand when new releases have backwards compatible APIs.

An API breakage is anything that modifies the name or call signature of an existing public-facing function or variable in the `Python` code in such a way that the change is not backwards compatible. For example, removing a `Python` keyword argument is an API breakage. However, adding one is not. Significant changes to the behavior of a function also count as an API breakage (e.g. if an assumption is changed that causes different results to be produced by default). Fixing a bug that affects the output of a function does not count as an API breakage, unless the fix modifies function names and arguments too as described above.

If the API is broken, the CCL major version number must be incremented (e.g. from `v1.5.0` to `v2.0.0`), and a new tagged release should be made shortly after the changes are pushed to `master`. The new release must include notes in `CHANGELOG.md` that describe how the API has been changed. The aim is to make it clear to users how their CCL-based code might be affected if they update to the latest version, especially if the update is likely to break something. All API changes should be discussed with the CCL team before being pushed to the `master` branch.



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## Navigating the Code

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The CCL package is laid out as follows.

- `.travis/`: helper scripts for running tests on Travis-CI
- `benchmarks/`: source code and data for the benchmark tests, see *Writing and Running Benchmarks* for more details.
- `cmake/`: CMake modules for building the CCL C layer
- `doc/`: latex source for the CCL note and the CCL paper
- `examples/`: (possible outdated) examples of how to use CCL
- `include/`: CCL C layer header files
- `pyccl/`: the CCL Python package
- `readthedocs/`: the CCL Read the Docs source
- `src/`: the CCL C layer source code
- `setup.py`: the Python install script
- `CMakeLists.txt`: the CMake installation configuration
- `.travis.yml`: the Travis-CI configuration
- `CHANGELOG.md`: the CCL log of changes to the code

### 7.1 Locations of Core Cosmological Quantities

Here we describe briefly the locations of the computations of core cosmological quantities. Usually each of these C files has a corresponding Python file, SWIG interface file, and C header file. However this is not always true for various reasons.

- `ccl_background.c`: computations of growth functions, the Hubble function and distances
- `ccl_core.c`: functions to handle cosmology structures and parameters

- `ccl_error.c`: functions to help handle C-layer errors
- `ccl_bbks.c`: the BBKS transfer function
- `ccl_f1d.c`: 1-d interpolations in C
- `ccl_f2d.c`: 2-d interpolations in C
- `ccl_power.c`: code to spline and initialize the power spectra and transfer functions
- `ccl_bcm.c`: code to compute the BCM model for baryonic effects
- `ccl_eh.c`: code to compute the Eisenstein and Hu (1998) transfer function approximation
- `ccl_musigma.c`: code to properly normalize input linear power spectra for the  $\mu$ -Sigma modified gravity model
- `ccl_cls.c`: code to compute angular power spectra from 3-d power spectra
- `ccl_massfunc.c`: code for the halo mass function and halo bias models, also contains code to spline the linear power spectrum variance in top-hat windows  $\sigma(R)$
- `ccl_neutrinos.c`: code to compute the neutrino masses from their cosmological density and vice versa.
- `ccl_emu17.c`: code to compute the Cosmic Emu emulator for the matter power spectrum
- `ccl_correlation.c`: code to compute correlation functions from 2-d and 3-d power spectra
- `ccl_halomod.c`: code to compute halo model approximations to the power spectrum, also contains models for the halo mass-concentration relationship
- `ccl_halofit.c`: code to compute the HALOFIT approximation for the non-linear matter power spectrum
- `ccl_haloprofile.c`: code to compute common approximations to halo mass density profiles
- `ccl_tracers.c`: code to compute various kernels for tracers of large-scale structure (e.g., weak lensing kernels, galaxy clustering kernels, etc.)
- `ccl_fftlog.c`: an implementation of the FFTLog algorithm for fast transforms between Fourier and real space quantities



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## Understanding the Python-C Interface

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The Python interface to the CCL C code is built using SWIG, which automatically scans the CCL C headers and builds a matching interface in Python. The autogenerated SWIG interface can be accessed through the `pyccl.ccllib` module. The actual CCL API in Python is a more user-friendly wrapper that has been written on top of the SWIG-generated code.

### 8.1 Key Parts of SWIG Wrapper

The key parts/conventions of the SWIG wrapper are as follows:

- Interface `.i` files: These are kept in the `pyccl/` directory, and tell SWIG which functions to extract from the C headers. There are also commands in these files to generate basic function argument documentation, and to remove the `ccl_` prefix from function names. The interface files also contain code that tells SWIG how to convert C array arguments to numpy arrays. For certain functions, this code may also contain a simple loop to vectorize the function.
- Main interface file `pyccl/ccl.i`: This file imports all of the other interface files. Most of the CCL source files (e.g. `ccl_core.c`) have their own interface file too. For other files, mostly containing support/utility functions, SWIG only needs the C header (`.h`) file to be specified in the main `ccl.i` file.
- Internal CCL C-level global state: All global state in the CCL library (e.g., whether or not the power spectra splines are initialized and calling the function to initialize them) is controlled by the Python code. This convention ensures that when the C code is running, all data needed already exists. It also allows us to more easily use OpenMP in the C layer, avoiding the problem of having to manage the global state from more than one thread. In practice, this means that before you call the CCL C library from Python, you need to check to make sure that any internal C data you need has been initialized. The `pyccl.Cosmology` object has methods to help with this (e.g., `compute_distances()`).

## 8.2 Error Handling

Errors in CCL happen both in the C and Python code. For the Python code, one should simply raise the appropriate error, often `CLError`. Error handling in the C code is a bit more subtle because the C code cannot (currently) raise Python exceptions directly.

Instead, CCL takes the convention that each C function passes back or returns a `status` value. Non-zero values indicate an error. Further, certain values have special meanings that are defined in the `include/ccl_error.h` header file. The Python file `pyccl/_types.py` contains translations of the C header macros into Python strings. These translations are used to translate the numerical error codes returned by the C code into something more human readable.

Further, in the CCL C layer, functions can write information about errors into a string held by the C version of the `pyccl.Cosmology` structure. The Python layer can then read the value of this string and raise it with a Python error when a non-zero status is returned.

Using these two mechanisms, Python functions in the CCL Python API can check for errors in the C layer and report back useful information to the user.

## 8.3 Example Python and C Code

Putting together all of the information above, here is example code based on the CCL `pyccl_bcm` module. Note that the code snippets here may be out of date relative to their current form in the repository.

### 8.3.1 C Header File `include/ccl_bcm.h`

```

/** @file */
#ifndef __CCL_BCM_H_INCLUDED__
#define __CCL_BCM_H_INCLUDED__

CCL_BEGIN_DECLS

/**
 * Correction for the impact of baryonic physics on the matter power spectrum.
 * Returns  $f(k,a)$  [dimensionless] for given cosmology, using the method specified for
 * the baryonic transfer function.
 *  $f(k,a)$  is the fractional change in the nonlinear matter power spectrum from the
 * Baryon Correction Model (BCM) of Schenider & Teyssier (2015). The parameters of the
 * model are passed as part of the cosmology class.
 * @param cosmo Cosmology parameters and configurations, including baryonic
 * parameters.
 * @param k Fourier mode, in [1/Mpc] units
 * @param a scale factor, normalized to 1 for today
 * @param status Status flag. 0 if there are no errors, nonzero otherwise.
 * For specific cases see documentation for ccl_error.c
 * @return  $f(k,a)$ .
 */
double ccl_bcm_model_fka(ccl_cosmology * cosmo, double k, double a, int *status);

CCL_END_DECLS

#endif

```

Notice that the first argument is a C-level cosmology structure, the order of the arguments for wavenumber and scale factor, and that the last argument is a pointer to the `status` variable.

This C header file is then included in the `include/ccl.h` header file via `#include "ccl_bcm.h"`.

### 8.3.2 C Source File `src/ccl_bcm.c`

```
#include <math.h>
#include "ccl.h"

/* BCM correction */
// See Schneider & Teyssier (2015) for details of the model.
double ccl_bcm_model_fka(ccl_cosmology * cosmo, double k, double a, int *status) {
    double fkz;
    double b0;
    double bfunc, bfunc4;
    double kg;
    double gf, scomp;
    double kh;
    double z;

    if (a < 0) {
        *status = CCL_ERROR_PARAMETERS;
        return NaN;
    }

    // compute the BCM model here
    fkz = ...
    return fkz;
}
```

Here we see that if we encounter an error, the `status` variable is set and some fiducial value is returned. (Note that the check above does not actually exist in the main CCL source file.)

### 8.3.3 SWIG Interface File `pyccl/ccl_bcm.i`

```
%module ccl_bcm

%{
/* put additional #include here */
%}

// Enable vectorised arguments for arrays
%apply (double* IN_ARRAY1, int DIM1) {(double* k, int nk)};
%apply (int DIM1, double* ARGOUT_ARRAY1) {(int nout, double* output)};

#include "../include/ccl_bcm.h"

/* The python code here will be executed before all of the functions that
follow this directive. */
%feature("pythonprepend") %{
    if numpy.shape(k) != (nout,):
        raise CCLError("Input shape for `k` must match `(nout,)!")
%}

%inline %{
void bcm_model_fka_vec(ccl_cosmology * cosmo, double a, double* k, int nk,
                      int nout, double* output, int* status) {
```

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```

    for(int i=0; i < nk; i++){
        output[i] = ccl_bcm_model_fka(cosmo, k[i], a, status);
    }
}

%}

/* The directive gets carried between files, so we reset it at the end. */
%feature("pythonprepend") %{ %}

```

This SWIG interface file contains several examples of important features in writing SWIG interfaces.

- We have declared some inline C code to enable fast, vectorized computations of the BCM model.
- We have used the `numpy.i` type signatures, described in their [documentation](#) to enable vectorized inputs and outputs. The `pyccl/ccl.i` interface file defines a global `numpy` type signature for the `status` variable.
- We have used the SWIG `pythonprepend` feature to add a check on the sizes of the input and output arrays to ensure that we do not access memory out of bounds.
- We made sure the module name at the top matches the C source file.
- We made sure to include the C header file from the right relative path.

Finally, this SWIG interface file is included in the `pyccl/ccl.i` interface file.

### 8.3.4 Python Module `pyccl/bcm.py`

```

from . import cclib as lib
from .pyutils import _vectorize_fn2

def bcm_model_fka(cosmo, k, a):
    """The BCM model correction factor for baryons.

    .. note:: BCM stands for the "baryonic correction model" of Schneider &
        Teyssier (2015; https://arxiv.org/abs/1510.06034). See the
        `DESC Note <https://github.com/LSSTDESC/CCL/blob/master/doc/0000-ccl\_note/main.pdf>`_
        for details.

    .. note:: The correction factor is applied multiplicatively so that
        `P_corrected(k, a) = P(k, a) * factor(k, a)`.

    Args:
        cosmo (:obj:`Cosmology`): Cosmological parameters.
        k (float or array_like): Wavenumber;  $\text{Mpc}^{-1}$ .
        a (float): Scale factor.

    Returns:
        float or array_like: Correction factor to apply to the power spectrum.
    """
    return _vectorize_fn2(lib.bcm_model_fka,
                          lib.bcm_model_fka_vec, cosmo, k, a)

```

This file defines the actual API for the BCM model in CCL. It is the function signature and location of this function, along with what values it is supposed to return, that defines the API. Changes to any of the underlying C code or even the helper Python functions does not constitute an API breakage.

There are a few other features to note.

- We have written a complete, Sphinx-compatible docstring on the module.
- We are using the CCL helper function `_vectorize_fn2` to call the SWIG-generated interfaces `pyccl.cllib.bcm_model_fka` and `pyccl.cllib.bcm_model_fka_vec`.
- If any data needed to be initialized before calling the SWIG interfaces, we would need to initialize it by calling a function before `vectorize_fn2`. See the `pyccl.background` module for an example.

Finally, let's take a look at the implementation of the function `vectorize_fn2`

```
def _vectorize_fn2(fn, fn_vec, cosmo, x, z, returns_status=True):

    """Generic wrapper to allow vectorized (1D array) access to CCL functions with
    one vector argument and one scalar argument, with a cosmology dependence.

    Args:
        fn (callable): Function with a single argument.
        fn_vec (callable): Function that has a vectorized implementation in
            a .i file.
        cosmo (ccl_cosmology or Cosmology): The input cosmology which gets
            converted to a ccl_cosmology.
        x (float or array_like): Argument to fn.
        z (float): Scalar argument to fn.
        returns_stats (bool): Indicates whether fn returns a status.

    """
    # Access ccl_cosmology object
    cosmo_in = cosmo
    cosmo = cosmo.cosmo
    status = 0

    # If a scalar was passed, convert to an array
    if isinstance(x, int):
        x = float(x)
    if isinstance(x, float):
        # Use single-value function
        if returns_status:
            f, status = fn(cosmo, x, z, status)
        else:
            f = fn(cosmo, x, z)
    elif isinstance(x, np.ndarray):
        # Use vectorised function
        if returns_status:
            f, status = fn_vec(cosmo, z, x, x.size, status)
        else:
            f = fn_vec(cosmo, z, x, x.size)
    else:
        # Use vectorised function
        if returns_status:
            f, status = fn_vec(cosmo, z, x, len(x), status)
        else:
            f = fn_vec(cosmo, z, x, len(x))

    # Check result and return
    check(status, cosmo_in)
    return f
```

This function does a few nice things for us

- It handles multiple input argument types, casting them to the right type to be passed to the SWIG-generated interface functions.
- At the end, it calls another function `check`. It is this function that checks the `status` variable and if it is non-zero, raises an error using the error string passed back from the C library.

You will find quite a few versions of this function in `pyccl.pyutils` for use in calling the SWIG-generated API for different numbers of arguments.

---

## Developer Installation

---

To develop new code for CCL, you need to install it using `pip`'s development install. This installation method creates a symbolic link between your `Python site-packages` directory and the copy of CCL you are working on locally. Thus when you change CCL Python code, you do not need to reinstall CCL in order for the changes to be visible system-wide. Note, if you change the CCL C code, you will need to force CCL to recompile the code (and copy the resulting `.so` into the Python package) by rerunning the command below.

To install CCL using a `pip` developer installation, you can execute

```
$ pip install --no-deps -e .
```

from the top-level directory in the repository. You will need `CMake` in order to install CCL in this way. See [Getting CMake](#) for help installing `CMake` if you do not already have it. In order to run the tests, you will need `CAMB`, `CLASS`, and `FAST-PT` installed. See the instructions for [Getting a Boltzmann Code](#) and [Getting FAST-PT](#) for details.

### 9.1 C-layer Dependencies and Requirements

CCL has several C dependencies. The `CMake` build will download and compile these automatically if they are not present on your system. However, if you do have them installed locally in a spot accessible to `CMake`, the local versions will be used.

These dependencies are

- GNU Scientific Library [GSL](#), version 2.1 or above
- [FFTW3](#) version 3.1 or above
- [CLASS](#) version 2.6.3 or above
- [SWIG](#)

## 9.2 Uninstalling CCL in Developer Mode

To uninstall CCL in developer mode, simply type

```
$ pip uninstall pyccl
```

## 9.3 Bootstrapping a CCL Development Environment with conda

One of the easier ways to get started with CCL development is to use `conda-forge` to provide the third-party requirements above and the necessary compilers. The following commands will get you started with a `conda-forge`-based development environment. Note that before you start, make sure to follow the [conda-forge instructions](#) for use and that your `PYTHONPATH` variable is not set.

Then do the following

```
$ conda create -n ccl-dev compilers cmake swig pyccl pytest flake8
$ conda activate ccl-dev
$ conda uninstall pyccl --force
$ git clone https://github.com/LSSTDESC/CCL.git
$ cd CCL
$ pip install --no-deps -e .
```

This set of commands leaves a copy of the compiled C extension in the checked out copy of the code, e.g.,

```
$ ls pyccl/*.so
pyccl/_ccllib.so
```

If you make changes to the C library or checkout a new branch, simply rerun `pip install --no-deps -e .` to rebuild the library.



---

## Development Workflow

---

CCL development proceeds via pull requests on GitHub. In short, the code base is forked on GitHub, a new change is pushed to a new branch, and then a pull request is issued by the developer. Once a pull request is issued, CCL uses Travis-CI to automatically run the benchmark/unit tests and the linter. Please read the sections below for guidance on how to modify the source code, test, and then document your modifications.

### 10.1 Working on the Python library

After completing the *Developer Installation*, you can change the Python library in your local copy of CCL. Any changes you make will be visible in Python after you restart your interpreter. A typical workflow is to make some change, rerun a failing benchmark or unit test, etc. until you've completed your new feature and/or fixed a bug. See *Writing and Running Benchmarks* and *Writing and Running Unit Tests* for instructions on how to run these test suites. Please add unit tests and benchmarks as appropriate for any new functionality. You should also make sure to run the linter by following the instructions in *Linting with flake8*. Finally, after you are satisfied with your new code, make sure to follow *Updating the Changelog and Documentation* in order to properly document your new additions.

### 10.2 Adding New C-level Features to CCL

Before adding new features to the CCL C code, please read *Understanding the Python-C Interface* in order to understand how the Python and C codes interact.

The following steps are needed to add a new source file `ccl_newfile.c` and header `ccl_newfile.h` to the library.

1. Put `ccl_newfile.c` in the `src` directory.
2. Put `ccl_newfile.h` in the `include` directory.
3. Make sure to add a C-level include of your new header to `include/ccl.h`.
4. Add the new source file `ccl_newfile.c` to the `CCL_SRC` variable in `CMakeLists.txt`.

5. Write a `ccl_newfile.i` SWIG interface file for the new functions. This file gets placed in the `pyccl` directory. You may need to consult another CCL developer for help with the SWIG interface files.
6. Add your new SWIG interface file `ccl_newfile.i` to the list of includes in the `pyccl/ccl.i` file.
7. Write the public Python APIs for your new function in a file called `pyccl/newfile.py`. This Python package should access the C code you wrote from the new functions in `pyccl.cllib`.
8. Import your new functions into the `pyccl/__init__.py` file as needed.
9. Add unit tests and benchmarks as appropriate for the new code. See *Writing and Running Benchmarks* and *Writing and Running Unit Tests* for details.
10. Make sure to run the linter by following the instructions in *Linting with flake8*.
11. Follow *Updating the Changelog and Documentation* in order to properly document your new additions.

Occasionally, modifications made correctly as described above will still not function properly. This might be due to multiple `pyccl` installation files not being properly overwritten, and the Python interpreter getting confused. At this point it is often best to resort to the “nuclear option” of deleting all Python files related to `pyccl` and starting from scratch. The procedure is as follows:

1. Execute `pip uninstall pyccl` (possibly multiple times) to remove all installed versions of `pyccl`.
2. Delete the compiled C files.
  - Execute `rm -r build/` to delete the build directory.
  - Execute `rm pyccl/ccl_wrap.c pyccl/cllib.py` to delete the autogenerated SWIG files.
  - Check various locations for the Python `site-packages` directory for any `pyccl` files and delete them.
3. Reinstall CCL according to the *Developer Installation* instructions.

## 10.3 Updating the Changelog and Documentation

Please follow the following guidelines for documenting changes to CCL:

- New features and bug fixes should be documented in the `CHANGELOG.md` with a brief description and the GitHub pull request number.
- Any new derivations/math essential to understanding a new CCL feature should be documented in the CCL note. See `:ref:cclnote` for instructions on how to modify and compile it.
- All additions to the Python public API should have Python docstrings. These are written in Sphinx compatible format so that they can be incorporated into the CCL Read the Docs pages. See the current Python docstrings in the Python source for examples.
- Additions to the C code should be documented/commented so that other CCL developers can understand the code.

## 10.4 Linting with flake8

CCL uses `flake8` to ensure that the Python code has a consistent style. `flake8` is available via `pip` or `conda` via `[pip|conda] install flake8`. You can run this tool locally by executing

```
$ flake8 pyccl
```

Any problems will be printed to `STDOUT`. No output indicates that `flake8` has succeeded.

## 10.5 Debug mode in Python

Because of the way the `Python` wrapper handles exceptions that occur inside the `C` code, by default users will only see error messages for the most recent error that occurs. If multiple errors occurred during a CCL function call, all but the most recent error message will be overwritten. This convention can make it difficult to debug the root cause of a problem.

To help with debugging this kind of issue, you can enable debug mode in the `Python` wrapper. To do so, simply call `pyccl.debug_mode(True)`. This will cause the `Python` wrapper to print all `C` error messages to `STDERR` whenever they occur. `Python` exceptions will only be raised for the most recent error, as before. (Note that Jupyter notebooks do not print `C` `STDERR` messages by default.)

## 10.6 Continuous Integration with Travis-CI

Travis-CI is a continuous integration service that reads the file `.travis.yml` file in the repository and then runs the benchmarks/unit tests. More details on Travis-CI can be found here: <https://docs.travis-ci.com/user/getting-started/>.

Every time you push a commit, Travis-CI will automatically try to build the libraries with your new changes and run the benchmark/unit tests. You can check the status of your builds by following the links from the pull request page. If your build errors or fails, you can scroll through the log to find out what went wrong. Warnings from `flake8` will result in the tests not passing. If your additions require new dependencies, make sure that you include them in the `conda` environments defined in `.travis/install.sh`.

## 10.7 Deploying a New Release

When cutting a new release, the procedure is as follows:

1. Make sure any API changes are documented in `CHANGELOG.md`
2. Commit to master
3. Create a new release from the GitHub interface here: <https://github.com/LSSDESC/CCL/releases/new>
4. Manually create a source distribution from the root CCL folder:

```
$ python setup.py sdist
```

This command will create a `.tar.gz` file in the `dist` folder. CAREFUL!!! Only build and upload the source distribution, not a binary wheel!

5. Upload source distribution to PyPi using `twine` (can be installed using `pip` or `conda`):

```
$ twine upload dist/pyccl-x.x.x.tar.gz
```

Make sure your `twine` and `setuptools` packages are up to date, otherwise the markdown formatting of the `README.md` will not be correctly processed on the CCL PyPi page.

6. The `conda-forge` automated release bots will detect the new PyPi release and automatically make a pull request on the CCL feedstock. Once this pull request is merged, the new CCL release will be available on `conda` after a few hours.
7. Rebuild and redeploy the Read the Docs pages per the instructions in *Building the Read the Docs Documentation*. Note that you may need to adjust the major version number in `readthedocs/conf.py` if the new version has a major version number bump.

A CCL administrator will need to complete the steps above.

## 10.8 Building the Read the Docs Documentation

To build the Read the Docs documentation, follow the following steps:

```
$ cd readthedocs
$ make clean
$ make html
```

You can then inspect the outputs in `readthedocs/_build/index.html` to make sure the formatting is correct. Finally, contact the [CCL administrators](#) to redeploy the live documentation.

## 10.9 Building the CCL Note

The CCL note is a latex'ed document located in `doc/0000-ccl_note`. It is used to document the scientific content of the CCL library. Note that documentation of the actual APIs and code should reside in the Python doc strings and other code comments.

To compile the CCL note, type `make` in the `doc/0000-ccl_note` directory.

If you need to modify the note, the files to modify are:

- `authors.csv`: To document your contribution.
- `main.tex`: To detail the changes to the library.
- `main.bib`: To add new references.

---

## Writing and Running Unit Tests

---

CCL uses the `pytest` package to run a suite of unit tests. This package can be installed via `pip` or `conda` with `[pip|conda] install pytest`.

### 11.1 Running the Unit Tests

To run the unit tests, execute

```
pytest -vv pyccl
```

from the top-level repository directory. Any errors will be reported at the end.

Other useful `pytest` options include

- `-k <name of test>`: adding this option with the name of the test will force `pytest` to only run that test
- `-s`: this option makes `pytest` print all output to `STDOUT` instead of its usual behavior of suppressing output
- `-x`: this option forces `pytest` to stop after the first failed test
- `--pdb`: this option will launch the `Python` debugger for failed tests, usually you want to combine it with `-s -x -k <name of test>` in order to debug a single failed test

### 11.2 Writing Unit Tests

Please follow the following guidelines when writing unit tests.

1. All unit tests should be written as modules in the `pytest/tests` submodule.
2. Each unit test is a function that does some operation with CCL and then uses a `Python assert` statement. A unit test is marked by `pytest` as failed when the `assert` statement fails.
3. The unit tests should be fast, ideally less than a second or so. This requirement means avoiding running `CLASS` or `CAMB` when it is not needed.

4. The unit tests file should have a name that matches the python module it is testing (e.g., `pyccl/tests/test_bcm.py` for `pyccl/bcm.py`).
5. The unit test function itself should have a name that starts with `test_` and is also descriptive.

An example of a unit test would be a file at `pyccl/tests/test_core.py` with the test

```
import numpy as np
import pyccl

def test_cosmology_sigma8_consistent():
    cosmo = pyccl.Cosmology(
        Omega_c=0.25, Omega_b=0.05, h=0.7, sigma8=0.8, n_s=0.95,
        transfer_function='bbks')
    assert np.allclose(pyccl.sigma8(cosmo), 0.8)
```

## 11.3 Building and Running CCL's C Unit Tests

CCL has a few vestigial unit tests written in C. Once you have `CMake` installed (see [Getting CMake](#)), you can build them with the following commands from the top-level CCL directory

```
$ mkdir -p build
$ cd build
$ cmake ..
$ make check_ccl
```

Then you can run the tests via

```
$ ./check_ccl
```

---

## Writing and Running Benchmarks

---

Nearly every new feature in CCL is benchmarked against an independent implementation. If you are adding a new feature, make sure someone can provide you with an independent output for cross-checks. Independent codes should be publicly available and a script to run them should be provided such that the user can reproduce the benchmarks.

### 12.1 Running the Benchmarks

After CCL is installed, the benchmarks can be run by executing

```
$ pytest -vv benchmarks
```

from the top-level directory of the repository. The *Writing and Running Unit Tests* section contains useful hints on using `pytest` to debug individual tests/benchmarks.

### 12.2 Writing a Benchmark

Benchmarks in CCL follow the `pytest` conventions for the CCL unit tests, but are located in the `benchmarks/` directory. Any data needed for the benchmark should be added to the `benchmarks/data` directory. Code to produce the benchmark data can be put in `benchmarks/data/code`. If it cannot be included in the repository, then a link on the [wiki](#) is acceptable.

The benchmark itself should read the data in the `benchmarks data` directory and then compare to the same computation done in CCL. Here is an example benchmark testing the CCL BBKS transfer function (located in the file `benchmarks/test_bbks.py`)

```
import numpy as np
import pycccl as ccl
import pytest

BBKS_TOLERANCE = 1.0e-5
```

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```
@pytest.mark.parametrize(
    'model,w0,wa',
    [(1, -1.0, 0.0),
     (2, -0.9, 0.0),
     (3, -0.9, 0.1)])
def test_bbks(model, w0, wa):
    cosmo = ccl.Cosmology(
        Omega_c=0.25,
        Omega_b=0.05,
        h=0.7,
        sigma8=0.8,
        n_s=0.96,
        Neff=0,
        m_nu=0.0,
        w0=w0,
        wa=wa,
        T_CMB=2.7,
        m_nu_type='normal',
        Omega_g=0,
        Omega_k=0,
        transfer_function='bbks',
        matter_power_spectrum='linear')

    data = np.loadtxt('./benchmarks/data/model%d_pk.txt' % model)

    k = data[:, 0] * cosmo['h']
    for i in range(6):
        a = 1.0 / (1.0 + i)
        pk = data[:, i+1] / (cosmo['h']**3)
        pk_ccl = ccl.linear_matter_power(cosmo, k, a)
        err = np.abs(pk_ccl/pk - 1)
        assert np.allclose(err, 0, rtol=0, atol=BBKS_TOLERANCE)
```

Note that the benchmarks are executed from the top-level of the repository so that the file paths for data are benchmarks/data/<data file>.



---

## Notation, Models and Other Cosmological Conventions

---

The documentation here provides a brief description of CCL and its contents. For a more thorough description of the underlying equations CCL implements, see the [CCL note](#) and the [CCL paper](#).

### 13.1 Cosmological Parameters

CCL uses the following parameters to define the cosmological model.

#### 13.1.1 Background Parameters

- `Omega_c`: the density fraction at  $z=0$  of CDM
- `Omega_b`: the density fraction at  $z=0$  of baryons
- `h`: the Hubble constant in units of 100 Mpc/km/s
- `Omega_k`: the curvature density fraction at  $z=0$
- `Omega_g`: the density of radiation (not including massless neutrinos)
- `w0`: first order term of the dark energy equation of state
- `wa`: second order term of the dark energy equation of state

#### 13.1.2 Power Spectrum Normalization

The power spectrum normalization is given either as `A_s` (i.e., the primordial amplitude) or as `sigma8` (i.e., a measure of the amplitude today). Note that not all transfer functions support specifying a primordial amplitude.

- `sigma8`: the normalization of the power spectrum today, given by the RMS variance in spheres of 8 Mpc/h
- `A_s`: the primordial normalization of the power spectrum at  $k=0.05 \text{ Mpc}^{-1}$

### 13.1.3 Relativistic Species

- `Neff`: effective number of massless+massive neutrinos present at recombination
- `m_nu`: the total mass of massive neutrinos or the masses of the massive neutrinos in eV
- `m_nu_type`: how to interpret the `m_nu` argument, see the *options* below
- `T_CMB`: the temperature of the CMB today

### 13.1.4 Modified Gravity Parameters

- `mu_0` and `sigma_0`: the parameters of the scale-independent  $\mu - \Sigma$  modified gravity model
- `df_mg` and `z_mg`: arrays of perturbations to the GR growth rate  $f$  as a function of redshift

## 13.2 Supported Models for the Power Spectrum, Mass Function, etc.

`pyccl` accepts strings indicating which model to use for various physical quantities (e.g., the transfer function). The various options are as follows.

`transfer_function` options

- `None` : do not compute a linear power spectrum
- `'eisenstein_hu'`: the Eisenstein and Hu (1998) fitting function
- `'bbks'`: the BBKS approximation
- `'boltzmann_class'`: use CLASS to compute the transfer function
- `'boltzmann_camb'`: use CAMB to compute the transfer function (default)

`matter_power_spectrum` options

- `'halo_model'`: use a halo model
- `'halofit'`: use HALOFIT (default)
- `'linear'`: neglect non-linear power spectrum contributions
- `'emu'`: use the Cosmic Emu

`baryons_power_spectrum` options

- `'nobaryons'`: neglect baryonic contributions to the power spectrum (default)
- `'bcm'`: use the baryonic correction model

`mass_function` options

- `'tinker'`: the Tinker et al. (2008) mass function
- `'tinker10'`: the Tinker et al. (2010) mass function (default)
- `'watson'`: the Watson et al. mass function
- `'angulo'`: the Angulo et al. mass function
- `'shethtormen'`: the Sheth and Tormen mass function

`halo_concentration` options

- `'bhattacharya2011'`: Bhattacharya et al. (2011) relation

- ‘duffy2008’: Duffy et al. (2008) relation (default)
- ‘constant\_concentration’: use a constant concentration

`m_nu_type` options

This parameter specifies the model for massive neutrinos.

- ‘list’: specify each mass yourself in eV
- ‘normal’: use the normal hierarchy to convert total mass to individual masses (default)
- ‘inverted’: use the inverted hierarchy to convert total mass to individual masses
- ‘equal’: assume equal masses when converting the total mass to individual masses

`emulator_neutrinos` options

This parameter specifies how to handle inconsistencies in the treatment of neutrinos between the Cosmic Emu (equal masses) and other models.

- ‘strict’: fail unless things are absolutely consistent (default)
- ‘equalize’: redistribute the total mass equally before using the Cosmic Emu. This option may result in slight internal inconsistencies in the physical model assumed for neutrinos.

## 13.3 Controlling Splines and Numerical Accuracy

The internal splines and integration accuracy are controlled by the attributes of `Cosmology.cosmo.spline_params` and `Cosmology.cosmo.gsl_params`. These should be set after instantiation, but before the object is used. For example, you can set the generic relative accuracy for integration by executing `c = Cosmology(...); c.cosmo.gsl_params.INTEGRATION_EPSREL = 1e-5`. The default values for these parameters are located in `src/ccl_core.c`.

The internal splines are controlled by the following parameters.

- `A_SPLINE_NLOG`: the number of logarithmically spaced bins between `A_SPLINE_MINLOG` and `A_SPLINE_MIN`.
- `A_SPLINE_NA`: the number of linearly spaced bins between `A_SPLINE_MIN` and `A_SPLINE_MAX`.
- `A_SPLINE_MINLOG`: the minimum value of the scale factor splines used for distances, etc.
- `A_SPLINE_MIN`: the transition scale factor between logarithmically spaced spline points and linearly spaced spline points.
- `A_SPLINE_MAX`: the the maximum value of the scale factor splines used for distances, etc.
- `LOGM_SPLINE_NM`: the number of logarithmically spaced values in mass for splines used in the computation of the halo mass function.
- `LOGM_SPLINE_MIN`: the base-10 logarithm of the minimum halo mass for splines used in the computation of the halo mass function.
- `LOGM_SPLINE_MAX`: the base-10 logarithm of the maximum halo mass for splines used in the computation of the halo mass function.
- `LOGM_SPLINE_DELTA`: the step in base-10 logarithmic units for computing finite difference derivatives in the computation of the mass function.
- `A_SPLINE_NLOG_PK`: the number of logarithmically spaced bins between `A_SPLINE_MINLOG_PK` and `A_SPLINE_MIN_PK`.
- `A_SPLINE_NA_PK`: the number of linearly spaced bins between `A_SPLINE_MIN_PK` and `A_SPLINE_MAX`.

- `A_SPLINE_MINLOG_PK`: the minimum value of the scale factor used for the power spectrum splines.
- `A_SPLINE_MIN_PK`: the transition scale factor between logarithmically spaced spline points and linearly spaced spline points for the power spectrum.
- `K_MIN`: the minimum wavenumber for the power spectrum splines for analytic models (e.g., BBKS, Eisenstein & Hu, etc.).
- `K_MAX`: the maximum wavenumber for the power spectrum splines for analytic models (e.g., BBKS, Eisenstein & Hu, etc.).
- `K_MAX_SPLINE`: the maximum wavenumber for the power spectrum splines for numerical models (e.g., ComsicEmu, CLASS, etc.).
- `N_K`: the number of spline nodes per decade for the power spectrum splines.
- `N_K_3DCOR`: the number of spline points in wavenumber per decade used for computing the 3D correlation function.
- `ELL_MIN_CORR`: the minimum value of the spline in angular wavenumber for correlation function computations with FFTlog.
- `ELL_MAX_CORR`: the maximum value of the spline in angular wavenumber for correlation function computations with FFTlog.
- `N_ELL_CORR`: the number of logarithmically spaced bins in angular wavenumber between `ELL_MIN_CORR` and `ELL_MAX_CORR`.

The numerical accuracy of GSL computations is controlled by the following parameters.

- `N_ITERATION`: the size of the GSL workspace for numerical integration.
- `INTEGRATION_GAUSS_KRONROD_POINTS`: the Gauss-Kronrod quadrature rule used for adaptive integrations.
- `INTEGRATION_EPSREL`: the relative error tolerance for numerical integration; used if not specified by a more specific parameter.
- `INTEGRATION_LIMBER_GAUSS_KRONROD_POINTS`: the Gauss-Kronrod quadrature rule used for adaptive integrations on subintervals for Limber integrals.
- `INTEGRATION_LIMBER_EPSREL`: the relative error tolerance for numerical integration of Limber integrals.
- `INTEGRATION_DISTANCE_EPSREL`: the relative error tolerance for numerical integration of distance integrals.
- `INTEGRATION_SIGMAR_EPSREL`: the relative error tolerance for numerical integration of power spectrum variance integrals for the mass function.
- `ROOT_EPSREL`: the relative error tolerance for root finding used to invert the relationship between comoving distance and scale factor.
- `ROOT_N_ITERATION`: the maximum number of iterations used to for root finding to invert the relationship between comoving distance and scale factor.
- `ODE_GROWTH_EPSREL`: the relative error tolerance for integrating the linear growth ODEs.
- `EPS_SCALEFAC_GROWTH`: 10x the starting step size for integrating the linear growth ODEs and the scale factor of the initial condition for the linear growth ODEs.
- `HM_MMIN`: the minimum mass for halo model integrations.
- `HM_MMAX`: the maximum mass for halo model integrations.
- `HM_EPSABS`: the absolute error tolerance for halo model integrations.

- `HM_EPSREL`: the relative error tolerance for halo model integrations.
- `HM_LIMIT`: the size of the GSL workspace for halo model integrations.
- `HM_INT_METHOD`: the Gauss-Kronrod quadrature rule used for adaptive integrations for the halo model computations.

## 13.4 Specifying Physical Constants

The values of physical constants are set globally. These can be changed by assigning a new value to the attributes of `pyccl.physical_constants`. The following constants are defined and their default values are located in `src/ccl_core.c`. Note that the neutrino mass splittings are taken from Lesgourgues & Pastor (2012; 1212.6154). Also, see the [CCL note](#) for a discussion of the values of these constants from different sources.

basic physical constants

- `CLIGHT_HMPC`: speed of light /  $H_0$  in units of Mpc/h
- `GNEWT`: Newton's gravitational constant in units of  $m^3/Kg/s^2$
- `SOLAR_MASS`: solar mass in units of kg
- `MPC_TO_METER`: conversion factor for Mpc to meters.
- `PC_TO_METER`: conversion factor for parsecs to meters.
- `RHO_CRITICAL`: critical density in units of  $M_{\text{sun}}/h / (Mpc/h)^3$
- `KBOLTZ`: Boltzmann constant in units of J/K
- `STBOLTZ`: Stefan-Boltzmann constant in units of  $kg/s^3 / K^4$
- `HPLANCK`: Planck's constant in units  $kg m^2 / s$
- `CLIGHT`: speed of light in m/s
- `EV_IN_J`: conversion factor between electron volts and Joules
- `T_CMB`: temperature of the CMB in K
- `TNCDM`: temperature of the cosmological neutrino background in K

neutrino mass splittings

- `DELTAM12_sq`: squared mass difference between eigenstates 2 and 1.
- `DELTAM13_sq_pos`: squared mass difference between eigenstates 3 and 1 for the normal hierarchy.
- `DELTAM13_sq_neg`: squared mass difference between eigenstates 3 and 1 for the inverted hierarchy.



## 14.1 pyccl package

### 14.1.1 Subpackages

pyccl.halos package

Submodules

pyccl.halos.concentration module

**class** pyccl.halos.concentration.**Concentration** (*mass\_def=None*)

Bases: `object`

This class enables the calculation of halo concentrations.

**Parameters** **mass\_def** (*MassDef*) – a mass definition object that fixes the mass definition used by this  $c(M)$  parametrization.

**get\_concentration** (*cosmo, M, a, mdef\_other=None*)

Returns the concentration for input parameters.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **M** (*float or array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **mdef\_other** (*MassDef*) – the mass definition object that defines  $M$ .

**Returns** concentration.

**Return type** `float` or `array_like`

**name** = 'default'

**class** `pyccl.halos.concentration.ConcentrationBhattacharya13` (*mdef=None*)

Bases: `pyccl.halos.concentration.Concentration`

Concentration-mass relation by Bhattacharya et al. 2013 (arXiv:1112.5479). This parametrization is only valid for S.O. masses with  $\Delta = \Delta_{\text{vir}}$ , 200-matter and 200-critical. By default it will be initialized for  $\Delta = 200$ -critical.

**Parameters** `mdef` (*MassDef*) – a mass definition object that fixes the mass definition used by this `c(M)` parametrization.

`name = 'Bhattacharya13'`

**class** `pyccl.halos.concentration.ConcentrationConstant` (*c=1, mdef=None*)

Bases: `pyccl.halos.concentration.Concentration`

Constant concentration-mass relation.

**Parameters**

- `c` (*float*) – constant concentration value.
- `mdef` (*MassDef*) – a mass definition object that fixes the mass definition used by this `c(M)` parametrization. In this case it's arbitrary.

`name = 'Constant'`

**class** `pyccl.halos.concentration.ConcentrationDiemer15` (*mdef=None*)

Bases: `pyccl.halos.concentration.Concentration`

Concentration-mass relation by Diemer & Kravtsov 2015 (arXiv:1407.4730). This parametrization is only valid for S.O. masses with  $\Delta = 200$ -critical.

**Parameters** `mdef` (*MassDef*) – a mass definition object that fixes the mass definition used by this `c(M)` parametrization.

`name = 'Diemer15'`

**class** `pyccl.halos.concentration.ConcentrationDuffy08` (*mdef=None*)

Bases: `pyccl.halos.concentration.Concentration`

Concentration-mass relation by Duffy et al. 2008 (arXiv:0804.2486). This parametrization is only valid for S.O. masses with  $\Delta = \Delta_{\text{vir}}$ , 200-matter and 200-critical. By default it will be initialized for  $\Delta = 200$ -critical.

**Parameters** `mdef` (*MassDef*) – a mass definition object that fixes the mass definition used by this `c(M)` parametrization.

`name = 'Duffy08'`

**class** `pyccl.halos.concentration.ConcentrationKlypin11` (*mdef=None*)

Bases: `pyccl.halos.concentration.Concentration`

Concentration-mass relation by Klypin et al. 2011 (arXiv:1002.3660). This parametrization is only valid for S.O. masses with  $\Delta = \Delta_{\text{vir}}$ .

**Parameters** `mdef` (*MassDef*) – a mass definition object that fixes the mass definition used by this `c(M)` parametrization.

`name = 'Klypin11'`

**class** `pyccl.halos.concentration.ConcentrationPrada12` (*mdef=None*)

Bases: `pyccl.halos.concentration.Concentration`

Concentration-mass relation by Prada et al. 2012 (arXiv:1104.5130). This parametrization is only valid for S.O. masses with  $\Delta = 200$ -critical.



**Parameters** `mdef` (*MassDef*) – a mass definition object that fixes the mass definition used by this `c(M)` parametrization.

`name = 'Prada12'`

`pyccl.halos.concentration.concentration_from_name` (*name*)

Returns halo concentration subclass from name string

**Parameters** `name` (*string*) – a concentration name

**Returns** Concentration subclass corresponding to the input name.

## pyccl.halos.halo\_model module

```
class pyccl.halos.halo_model.HMCalculator (cosmo, massfunc, hbias,
                                          mass_def, log10M_min=8.0,
                                          log10M_max=16.0, nlog10M=128, inte-
                                          gration_method_M='simpson', k_min=1e-05)
```

Bases: `object`

This class implements a set of methods that can be used to compute various halo model quantities. A lot of these quantities will involve integrals of the sort:

$$\int dM n(M, a) f(M, k, a),$$

where  $n(M, a)$  is the halo mass function, and  $f$  is an arbitrary function of mass, scale factor and Fourier scales.

### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **massfunc** (*MassFunc*) – a mass function object.
- **hbias** (*HaloBias*) – a halo bias object.
- **mass\_def** (*MassDef*) – a mass definition object.
- **log10M\_min** (*float*) – logarithmic mass (in units of solar mass) corresponding to the lower bound of the integrals in mass. Default: 8.
- **log10M\_max** (*float*) – logarithmic mass (in units of solar mass) corresponding to the upper bound of the integrals in mass. Default: 16.
- **nlog10M** (*int*) – number of samples in  $\log(\text{Mass})$  to be used in the mass integrals. Default: 128.
- **integration\_method\_M** (*string*) – integration method to use in the mass integrals. Options: “simpson” and “spline”. Default: “simpson”.
- **k\_min** (*float*) – some of the integrals solved by this class will often be normalized by their value on very large scales. This parameter (in units of inverse Mpc) determines what is considered a “very large” scale. Default: 1E-5.

**I\_0\_1** (*cosmo, k, a, prof*)

Solves the integral:

$$I_1^0(k, a|u) = \int dM n(M, a) \langle u(k, a|M) \rangle,$$

where  $n(M, a)$  is the halo mass function, and  $\langle u(k, a|M) \rangle$  is the halo profile as a function of scale, scale factor and halo mass.

**Parameters**

- **cosmo** (*Cosmology*) – a Cosmology object.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **a** (*float*) – scale factor.
- **prof** (*HaloProfile*) – halo profile.

**Returns** integral values evaluated at each value of  $k$ .

**Return type** *float* or *array\_like*

**I\_0\_2** (*cosmo, k, a, prof1, prof\_2pt, prof2=None*)

Solves the integral:

$$I_2^0(k, a|u, v) = \int dM n(M, a) \langle u(k, a|M)v(k, a|M) \rangle,$$

where  $n(M, a)$  is the halo mass function, and  $\langle u(k, a|M)v(k, a|M) \rangle$  is the two-point moment of the two halo profiles.

**Parameters**

- **cosmo** (*Cosmology*) – a Cosmology object.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **a** (*float*) – scale factor.
- **prof** (*HaloProfile*) – halo profile.
- **prof\_2pt** (*Profile2pt*) – a profile covariance object returning the the two-point moment of the two profiles being correlated.
- **prof2** (*HaloProfile*) – a second halo profile. If *None*, *prof* will be used as *prof2*.

**Returns** integral values evaluated at each value of  $k$ .

**Return type** *float* or *array\_like*

**I\_1\_1** (*cosmo, k, a, prof*)

Solves the integral:

$$I_1^1(k, a|u) = \int dM n(M, a) b(M, a) \langle u(k, a|M) \rangle,$$

where  $n(M, a)$  is the halo mass function,  $b(M, a)$  is the halo bias, and  $\langle u(k, a|M) \rangle$  is the halo profile as a function of scale, scale factor and halo mass.

**Parameters**

- **cosmo** (*Cosmology*) – a Cosmology object.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **a** (*float*) – scale factor.
- **prof** (*HaloProfile*) – halo profile.

**Returns** integral values evaluated at each value of  $k$ .

**Return type** *float* or *array\_like*

**number\_counts** (*cosmo, sel, na=128, amin=None, amax=1.0*)

Solves the integral:

$$nc(sel) = \int dM \int da \frac{dV}{dad\Omega} n(M, a) sel(M, a)$$

where  $n(M, a)$  is the halo mass function, and  $sel(M, a)$  is the selection function as a function of halo mass and scale factor.

Note that the selection function is normalized to integrate to unity and assumed to represent the selection probability per unit scale factor and per unit mass.

#### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **sel** (*callable*) – function of mass and scale factor that returns the selection function. This function should take in floats or arrays with a signature `sel(m, a)` and return an array with shape `(len(m), len(a))` according to the numpy broadcasting rules.
- **na** (*int*) – number of samples in scale factor to be used in the integrals. Default: 128.
- **amin** (*float*) – the minimum scale factor at which to start integrals over the selection function. Default: value of `cosmo.cosmo.spline_params.A_SPLINE_MIN`
- **amax** (*float*) – the maximum scale factor at which to end integrals over the selection function. Default: 1.0

**Returns** the total number of clusters

**Return type** float

**profile\_norm** (*cosmo, a, prof*)

Returns  $I_1^0(k \rightarrow 0, a|u)$  (see `I_0_1()`).

#### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **a** (*float*) – scale factor.
- **prof** (*HaloProfile*) – halo profile.

**Returns** integral value.

**Return type** float or array\_like

`pyccl.halos.halo_model.halomod_Pk2D` (*cosmo, hmc, prof, prof\_2pt=None, prof2=None, p\_of\_k\_a=None, normprof1=False, normprof2=False, get\_1h=True, get\_2h=True, lk\_arr=None, a\_arr=None, extrap\_order\_lok=1, extrap\_order\_hik=2*)

Returns a *Pk2D* object containing the halo-model power spectrum for two quantities defined by their respective halo profiles. See `pk()` for more details about the actual calculation.

#### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **hmc** (*HMCcalculator*) – a halo model calculator.
- **prof** (*HaloProfile*) – halo profile.
- **prof\_2pt** (*Profile2pt*) – a profile covariance object returning the the two-point moment of the two profiles being correlated. If *None*, the default second moment will be used, corresponding to the products of the means of both profiles.

- **prof2** (*HaloProfile*) – a second halo profile. If *None*, *prof* will be used as *prof2*.
- **p\_of\_k\_a** (*Pk2D*) – a *Pk2D* object to be used as the linear matter power spectrum. If *None*, the power spectrum stored within *cosmo* will be used.
- **normprof1** (*bool*) – if *True*, this integral will be normalized by  $I_1^0(k \rightarrow 0, a|u)$  (see [I\\_0\\_1\(\)](#)), where *u* is the profile represented by *prof*.
- **normprof2** (*bool*) – if *True*, this integral will be normalized by  $I_1^0(k \rightarrow 0, a|v)$  (see [I\\_0\\_1\(\)](#)), where *v* is the profile represented by *prof2*.
- **get\_1h** (*bool*) – if *False*, the 1-halo term (i.e. the first term in the first equation above) won't be computed.
- **get\_2h** (*bool*) – if *False*, the 2-halo term (i.e. the second term in the first equation above) won't be computed.
- **a\_arr** (*array*) – an array holding values of the scale factor at which the halo model power spectrum should be calculated for interpolation. If *None*, the internal values used by *cosmo* will be used.
- **lk\_arr** (*array*) – an array holding values of the natural logarithm of the wavenumber (in units of  $\text{Mpc}^{-1}$ ) at which the halo model power spectrum should be calculated for interpolation. If *None*, the internal values used by *cosmo* will be used.
- **extrap\_order\_lok** (*int*) – extrapolation order to be used on k-values below the minimum of the splines. See *Pk2D*.
- **extrap\_order\_hik** (*int*) – extrapolation order to be used on k-values above the maximum of the splines. See *Pk2D*.

**Returns** halo model power spectrum.

**Return type** *Pk2D*

`pyccl.halos.halo_model.halomod_bias_1pt` (*cosmo, hmc, k, a, prof, normprof=False*)

Returns the mass-and-bias-weighted mean halo profile.

$$I_1^1(k, a|u) = \int dM n(M, a) b(M, a) \langle u(k, a|M) \rangle,$$

where  $n(M, a)$  is the halo mass function,  $b(M, a)$  is the halo bias, and  $\langle u(k, a|M) \rangle$  is the halo profile as a function of scale, scale factor and halo mass.

#### Parameters

- **cosmo** (*Cosmology*) – a *Cosmology* object.
- **hmc** (*HMCcalculator*) – a halo model calculator.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **a** (*float or array\_like*) – scale factor.
- **prof** (*HaloProfile*) – halo profile.
- **normprof** (*bool*) – if *True*, this integral will be normalized by  $I_1^0(k \rightarrow 0, a|u)$  (see [I\\_0\\_1\(\)](#)).

**Returns** integral values evaluated at each combination of *k* and *a*. The shape of the output will be  $(N_a, N_k)$  where  $N_k$  and  $N_a$  are the sizes of *k* and *a* respectively. If *k* or *a* are scalars, the corresponding dimension will be squeezed out on output.

**Return type** *float or array\_like*

`pyccl.halos.halo_model.halomod_mean_profile_1pt` (*cosmo*, *hmc*, *k*, *a*, *prof*, *normprof=False*)

Returns the mass-weighted mean halo profile.

$$I_1^0(k, a|u) = \int dM n(M, a) \langle u(k, a|M) \rangle,$$

where  $n(M, a)$  is the halo mass function, and  $\langle u(k, a|M) \rangle$  is the halo profile as a function of scale, scale factor and halo mass.

#### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **hmc** (*HMCcalculator*) – a halo model calculator.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **a** (*float or array\_like*) – scale factor.
- **prof** (*HaloProfile*) – halo profile.
- **normprof** (*bool*) – if *True*, this integral will be normalized by  $I_1^0(k \rightarrow 0, a|u)$ .

**Returns** integral values evaluated at each combination of  $k$  and  $a$ . The shape of the output will be  $(N_a, N_k)$  where  $N_k$  and  $N_a$  are the sizes of  $k$  and  $a$  respectively. If  $k$  or  $a$  are scalars, the corresponding dimension will be squeezed out on output.

**Return type** `float` or `array_like`

`pyccl.halos.halo_model.halomod_power_spectrum` (*cosmo*, *hmc*, *k*, *a*, *prof*, *prof\_2pt=None*, *prof2=None*, *p\_of\_k\_a=None*, *normprof1=False*, *normprof2=False*, *get\_1h=True*, *get\_2h=True*)

Computes the halo model power spectrum for two quantities defined by their respective halo profiles. The halo model power spectrum for two profiles  $u$  and  $v$  is:

$$P_{u,v}(k, a) = I_0^2(k, a|u, v) + I_1^1(k, a|u) I_1^1(k, a|v) P_{\text{lin}}(k, a)$$

where  $P_{\text{lin}}(k, a)$  is the linear matter power spectrum,  $I_1^1$  is defined in the documentation of `I_1_1_1()`, and  $I_0^2$  is defined in the documentation of `I_0_2()`.

#### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **hmc** (*HMCcalculator*) – a halo model calculator.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **a** (*float or array\_like*) – scale factor.
- **prof** (*HaloProfile*) – halo profile.
- **prof\_2pt** (*Profile2pt*) – a profile covariance object returning the the two-point moment of the two profiles being correlated. If *None*, the default second moment will be used, corresponding to the products of the means of both profiles.
- **prof2** (*HaloProfile*) – a second halo profile. If *None*, *prof* will be used as *prof2*.
- **p\_of\_k\_a** (*Pk2D*) – a *Pk2D* object to be used as the linear matter power spectrum. If *None*, the power spectrum stored within *cosmo* will be used.
- **normprof1** (*bool*) – if *True*, this integral will be normalized by  $I_1^0(k \rightarrow 0, a|u)$  (see `I_0_1()`), where  $u$  is the profile represented by *prof*.

- **normprof2** (*bool*) – if *True*, this integral will be normalized by  $I_1^0(k \rightarrow 0, a|v)$  (see `I_0_1()`), where  $v$  is the profile represented by *prof2*.
- **get\_1h** (*bool*) – if *False*, the 1-halo term (i.e. the first term in the first equation above) won't be computed.
- **get\_2h** (*bool*) – if *False*, the 2-halo term (i.e. the second term in the first equation above) won't be computed.

**Returns** integral values evaluated at each combination of  $k$  and  $a$ . The shape of the output will be  $(N_a, N_k)$  where  $N_k$  and  $N_a$  are the sizes of  $k$  and  $a$  respectively. If  $k$  or  $a$  are scalars, the corresponding dimension will be squeezed out on output.

**Return type** `float` or `array_like`

## pyccl.halos.hbias module

**class** `pyccl.halos.hbias.HaloBias` (*cosmo*, *mass\_def=None*, *mass\_def\_strict=True*)

Bases: `object`

This class enables the calculation of halo bias functions. We currently assume that all halo bias functions can be written as functions that depend on  $M$  only through  $\sigma_M$  (where  $\sigma_M^2$  is the overdensity variance on spheres with a radius given by the Lagrangian radius for mass  $M$ ). All sub-classes implementing specific parametrizations can therefore be simply created by replacing this class' `_get_bsigma` method.

### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object that fixes the mass definition used by this halo bias parametrization.
- **mass\_def\_strict** (*bool*) – if *False*, consistency of the mass definition will be ignored.

**get\_halo\_bias** (*cosmo*, *M*, *a*, *mdef\_other=None*)

Returns the halo bias for input parameters.

### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **M** (*float* or *array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **mdef\_other** (*MassDef*) – the mass definition object that defines  $M$ .

**Returns** halo bias.

**Return type** `float` or `array_like`

**name** = `'default'`

**class** `pyccl.halos.hbias.HaloBiasBhattacharyall` (*cosmo*, *mass\_def=None*,  
*mass\_def\_strict=True*)

Bases: `pyccl.halos.hbias.HaloBias`

Implements halo bias described in arXiv:1005.2239. This parametrization is only valid for 'fof' masses.

### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts FoF masses only. If *None*, FoF masses will be used.

- `mass_def_strict` (*bool*) – if False, consistency of the mass definition will be ignored.

`name = 'Bhattacharya11'`

`class pycc1.halos.hbias.HaloBiasSheth01` (*cosmo, mass\_def=None, mass\_def\_strict=True*)

Bases: `pycc1.halos.hbias.HaloBias`

Implements halo bias described in arXiv:astro-ph/9907024. This parametrization is only valid for ‘fof’ masses.

#### Parameters

- `cosmo` (*Cosmology*) – A Cosmology object.
- `mass_def` (*MassDef*) – a mass definition object. this parametrization accepts FoF masses only. If *None*, FoF masses will be used.
- `mass_def_strict` (*bool*) – if False, consistency of the mass definition will be ignored.

`name = 'Sheth01'`

`class pycc1.halos.hbias.HaloBiasSheth99` (*cosmo, mass\_def=None, mass\_def\_strict=True, use\_delta\_c\_fit=False*)

Bases: `pycc1.halos.hbias.HaloBias`

Implements halo bias described in 1999MNRAS.308..119S This parametrization is only valid for ‘fof’ masses.

#### Parameters

- `cosmo` (*Cosmology*) – A Cosmology object.
- `mass_def` (*MassDef*) – a mass definition object. this parametrization accepts FoF masses only. If *None*, FoF masses will be used.
- `mass_def_strict` (*bool*) – if False, consistency of the mass definition will be ignored.
- `use_delta_c_fit` (*bool*) – if True, use `delta_crit` given by the fit of Nakamura & Suto 1997. Otherwise use `delta_crit = 1.68647`.

`name = 'Sheth99'`

`class pycc1.halos.hbias.HaloBiasTinker10` (*cosmo, mass\_def=None, mass\_def\_strict=True*)

Bases: `pycc1.halos.hbias.HaloBias`

Implements halo bias described in arXiv:1001.3162.

#### Parameters

- `cosmo` (*Cosmology*) – A Cosmology object.
- `mass_def` (*MassDef*) – a mass definition object. this parametrization accepts SO masses with  $200 < \Delta < 3200$  with respect to the matter density. If *None*,  $\Delta = 200$  (matter) will be used.
- `mass_def_strict` (*bool*) – if False, consistency of the mass definition will be ignored.

`name = 'Tinker10'`

`pycc1.halos.hbias.halo_bias_from_name` (*name*)

Returns halo bias subclass from name string

**Parameters** `name` (*string*) – a halo bias name

**Returns** HaloBias subclass corresponding to the input name.

## pyccl.halos.hmfunc module

**class** pyccl.halos.hmfunc.**MassFunc** (*cosmo*, *mass\_def=None*, *mass\_def\_strict=True*)

Bases: `object`

This class enables the calculation of halo mass functions. We currently assume that all mass functions can be written as

$$\frac{dn}{d \log_{10} M} = f(\sigma_M) \frac{\rho_M}{M} \frac{d \log \sigma_M}{d \log_{10} M}$$

where  $\sigma_M^2$  is the overdensity variance on spheres with a radius given by the Lagrangian radius for mass  $M$ . All sub-classes implementing specific mass function parametrizations can therefore be simply created by replacing this class' `_get_fsigma` method.

#### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object that fixes the mass definition used by this mass function parametrization.
- **mass\_def\_strict** (*bool*) – if False, consistency of the mass definition will be ignored.

**get\_mass\_function** (*cosmo*, *M*, *a*, *mdef\_other=None*)

Returns the mass function for input parameters.

#### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **M** (*float or array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **mdef\_other** (*MassDef*) – the mass definition object that defines  $M$ .

**Returns** mass function  $dn/d \log_{10} M$  in units of  $\text{Mpc}^{-3}$  (comoving).

**Return type** `float` or `array_like`

**name** = 'default'

**class** pyccl.halos.hmfunc.**MassFuncAngulo12** (*cosmo*, *mass\_def=None*, *mass\_def\_strict=True*)

Bases: `pyccl.halos.hmfunc.MassFunc`

Implements mass function described in arXiv:1203.3216. This parametrization is only valid for 'fof' masses.

#### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts FoF masses only. If *None*, FoF masses will be used.
- **mass\_def\_strict** (*bool*) – if False, consistency of the mass definition will be ignored.

**name** = 'Angulo12'

**class** pyccl.halos.hmfunc.**MassFuncBocquet16** (*cosmo*, *mass\_def=None*, *mass\_def\_strict=True*, *hydro=True*)

Bases: `pyccl.halos.hmfunc.MassFunc`

Implements mass function described in arXiv:1502.07357.

#### Parameters



- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts SO masses with Delta = 200 (matter, critical) and 500 (critical). If *None*, Delta = 200 (matter) will be used.
- **mass\_def\_strict** (*bool*) – if *False*, consistency of the mass definition will be ignored.
- **hydro** (*bool*) – if *False*, use the parametrization found using dark-matter-only simulations. Otherwise, include baryonic effects (default).

**name** = 'Bocquet16'

```
class pycc1.halos.hmfunc.MassFuncDespali16 (cosmo, mass_def=None,
                                           mass_def_strict=True, ellipsoidal=False)
```

Bases: *pycc1.halos.hmfunc.MassFunc*

Implements mass function described in arXiv:1507.05627.

#### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts any SO masses. If *None*, Delta = 200 (matter) will be used.
- **mass\_def\_strict** (*bool*) – if *False*, consistency of the mass definition will be ignored.

**name** = 'Despali16'

```
class pycc1.halos.hmfunc.MassFuncJenkins01 (cosmo, mass_def=None,
                                           mass_def_strict=True)
```

Bases: *pycc1.halos.hmfunc.MassFunc*

Implements mass function described in astro-ph/0005260. This parametrization is only valid for 'fof' masses.

#### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts FoF masses only. If *None*, FoF masses will be used.
- **mass\_def\_strict** (*bool*) – if *False*, consistency of the mass definition will be ignored.

**name** = 'Jenkins01'

```
class pycc1.halos.hmfunc.MassFuncPress74 (cosmo, mass_def=None, mass_def_strict=True)
```

Bases: *pycc1.halos.hmfunc.MassFunc*

Implements mass function described in 1974ApJ...187..425P. This parametrization is only valid for 'fof' masses.

#### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts FoF masses only. If *None*, FoF masses will be used.
- **mass\_def\_strict** (*bool*) – if *False*, consistency of the mass definition will be ignored.

**name** = 'Press74'

```
class pycc1.halos.hmfunc.MassFuncSheth99 (cosmo, mass_def=None, mass_def_strict=True,
                                           use_delta_c_fit=False)
```

Bases: *pycc1.halos.hmfunc.MassFunc*

Implements mass function described in arXiv:astro-ph/9901122 This parametrization is only valid for ‘fof’ masses.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts FoF masses only. If *None*, FoF masses will be used.
- **mass\_def\_strict** (*bool*) – if False, consistency of the mass definition will be ignored.
- **use\_delta\_c\_fit** (*bool*) – if True, use delta\_crit given by the fit of Nakamura & Suto 1997. Otherwise use delta\_crit = 1.68647.

**name** = 'Sheth99'

```
class pycc1.halos.hmfunc.MassFuncTinker08 (cosmo, mass_def=None,
                                           mass_def_strict=True)
```

Bases: *pycc1.halos.hmfunc.MassFunc*

Implements mass function described in arXiv:0803.2706.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts SO masses with  $200 < \Delta < 3200$  with respect to the matter density. If *None*,  $\Delta = 200$  (matter) will be used.
- **mass\_def\_strict** (*bool*) – if False, consistency of the mass definition will be ignored.

**name** = 'Tinker08'

```
class pycc1.halos.hmfunc.MassFuncTinker10 (cosmo, mass_def=None,
                                           mass_def_strict=True)
```

Bases: *pycc1.halos.hmfunc.MassFunc*

Implements mass function described in arXiv:1001.3162.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts SO masses with  $200 < \Delta < 3200$  with respect to the matter density. If *None*,  $\Delta = 200$  (matter) will be used.
- **mass\_def\_strict** (*bool*) – if False, consistency of the mass definition will be ignored.

**name** = 'Tinker10'

```
class pycc1.halos.hmfunc.MassFuncWatson13 (cosmo, mass_def=None,
                                           mass_def_strict=True)
```

Bases: *pycc1.halos.hmfunc.MassFunc*

Implements mass function described in arXiv:1212.0095.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **mass\_def** (*MassDef*) – a mass definition object. this parametrization accepts fof and any SO masses. If *None*,  $\Delta = 200$  (matter) will be used.
- **mass\_def\_strict** (*bool*) – if False, consistency of the mass definition will be ignored.

```
name = 'Watson13'
```

```
pyccl.halos.hmfunc.mass_function_from_name(name)
```

Returns mass function subclass from name string

**Parameters** `name` (*string*) – a mass function name

**Returns** MassFunc subclass corresponding to the input name.

## pyccl.halos.massdef module

```
class pyccl.halos.massdef.MassDef(Delta, rho_type, c_m_relation=None)
```

Bases: `object`

Halo mass definition. Halo masses are defined in terms of an overdensity parameter  $\Delta$  and an associated density  $X$  (either the matter density or the critical density):

$$M = \frac{4\pi}{3} \Delta \rho_X R^3$$

where  $R$  is the halo radius. This object also holds methods to translate between  $R$  and  $M$ , and to translate masses between different definitions if a concentration-mass relation is provided.

### Parameters

- **Delta** (*float*) – overdensity parameter. Pass ‘vir’ if using virial overdensity.
- **rho\_type** (*string*) – either ‘critical’ or ‘matter’.
- **c\_m\_relation** (*function, optional*) – concentration-mass relation. Provided as a *Concentration* object, or a string corresponding to one of the supported concentration-mass relations. If *None*, no c(M) relation will be attached to this mass definition (and hence one can’t translate into other definitions).

```
get_Delta(cosmo, a)
```

Gets overdensity parameter associated to this mass definition.

### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **a** (*float*) – scale factor

**Returns** value of the overdensity parameter.

**Return type** `float`

```
get_mass(cosmo, R, a)
```

Translates a halo radius into a mass

$$M = \frac{4\pi}{3} \Delta \rho_X R^3$$

### Parameters

- **cosmo** (*Cosmology*) – A Cosmology object.
- **R** (*float or array\_like*) – halo radius in units of Mpc (physical, not comoving).
- **a** (*float*) – scale factor.

**Returns** halo mass in units of `M_sun`.

**Return type** `float` or `array_like`

**get\_radius** (*cosmo*, *M*, *a*)

Translates a halo mass into a radius

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **M** (*float* or *array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.

**Returns**

**halo radius in units of Mpc (physical, not comoving).**

**Return type** *float* or *array\_like*

**translate\_mass** (*cosmo*, *M*, *a*, *m\_def\_other*)

Translate halo mass in this definition into another definition

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **M** (*float* or *array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **m\_def\_other** (*MassDef*) – another mass definition.

**Returns** halo masses in new definition.

**Return type** *float* or *array\_like*

**class** `pyccl.halos.massdef.MassDef200c` (*c\_m*=*'Duffy08'*)

Bases: `pyccl.halos.massdef.MassDef`

*MassDef* class for the mass definition with  $\Delta=200$  times the critical density.

**Parameters** **c\_m** (*string*) – concentration-mass relation.

**class** `pyccl.halos.massdef.MassDef200m` (*c\_m*=*'Duffy08'*)

Bases: `pyccl.halos.massdef.MassDef`

*MassDef* class for the mass definition with  $\Delta=200$  times the matter density.

**Parameters** **c\_m** (*string*) – concentration-mass relation.

**class** `pyccl.halos.massdef.MassDefVir` (*c\_m*=*'Klypin11'*)

Bases: `pyccl.halos.massdef.MassDef`

*MassDef* class for the mass definition with  $\Delta=\Delta_{\text{vir}}$  times the critical density.

**Parameters** **c\_m** (*string*) – concentration-mass relation.

`pyccl.halos.massdef.convert_concentration` (*cosmo*, *c\_old*, *Delta\_old*, *Delta\_new*)

Computes the concentration parameter for a different mass definition. This is done assuming an NFW profile. The output concentration  $c_{\text{new}}$  is found by solving the equation:

$$f(c_{\text{old}})\Delta_{\text{old}} = f(c_{\text{new}})\Delta_{\text{new}}$$

where

$$f(x) = \frac{x^3}{\log(1+x) - x/(1+x)}$$

**Parameters**

- `cosmo` (*Cosmology*) – A Cosmology object.
- `c_old` (*float or array\_like*) – concentration to translate from.
- `Delta_old` (*float*) – Delta parameter associated to the input concentration. See description of the `MassDef` class.
- `Delta_new` (*float*) – Delta parameter associated to the output concentration.

**Returns** concentration parameter for the new mass definition.

**Return type** `float` or `array_like`

`pyccl.halos.massdef.mass2radius_lagrangian` (*cosmo, M*)

Returns Lagrangian radius for a halo of mass `M`. The lagrangian radius is defined as that enclosing the mass of the halo assuming a homogeneous Universe.

**Parameters**

- `cosmo` (*Cosmology*) – A Cosmology object.
- `M` (*float or array\_like*) – halo mass in units of `M_sun`.

**Returns** lagrangian radius in comoving Mpc.

**Return type** `float` or `array_like`

## pyccl.halos.profiles module

**class** `pyccl.halos.profiles.HaloProfile`

Bases: `object`

This class implements functionality associated to halo profiles. You should not use this class directly. Instead, use one of the subclasses implemented in CCL for specific halo profiles, or write your own subclass. *HaloProfile* classes contain methods to compute halo profiles in real (3D) and Fourier spaces, as well as the projected (2D) profile and the cumulative mean surface density.

A minimal implementation of a *HaloProfile* subclass should contain a method `_real` that returns the real-space profile as a function of cosmology, comoving radius, mass and scale factor. The default functionality in the base *HaloProfile* class will then allow the automatic calculation of the Fourier-space and projected profiles, as well as the cumulative mass density, based on the real-space profile using `FFTLg` to carry out fast Hankel transforms. See the CCL note for details. Alternatively, you can implement a `_fourier` method for the Fourier-space profile, and all other quantities will be computed from it. It is also possible to implement specific versions of any of these quantities if one wants to avoid the `FFTLg` calculation.

**cumul2d** (*cosmo, r\_t, M, a, mass\_def=None*)

Returns the 2D cumulative surface density as a function of cosmology, radius, halo mass and scale factor.

$$\Sigma(< R) = \frac{2}{R^2} \int dR' R' \Sigma(R')$$

**Parameters**

- `cosmo` (*Cosmology*) – a Cosmology object.
- `r` (*float or array\_like*) – comoving radius in Mpc.
- `M` (*float or array\_like*) – halo mass in units of `M_sun`.
- `a` (*float*) – scale factor.
- `mass_def` (*MassDef*) – a mass definition object.

**Returns** halo profile. The shape of the output will be  $(N_M, N_r)$  where  $N_r$  and  $N_m$  are the sizes of  $r$  and  $M$  respectively. If  $r$  or  $M$  are scalars, the corresponding dimension will be squeezed out on output.

**Return type** float or array\_like

**fourier** (*cosmo, k, M, a, mass\_def=None*)

Returns the Fourier-space value of the profile as a function of cosmology, wavenumber, halo mass and scale factor.

$$\rho(k) = \frac{1}{2\pi^2} \int dr r^2 \rho(r) j_0(kr)$$

#### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **M** (*float or array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **mass\_def** (*MassDef*) – a mass definition object.

**Returns** halo profile. The shape of the output will be  $(N_M, N_k)$  where  $N_k$  and  $N_m$  are the sizes of  $k$  and  $M$  respectively. If  $k$  or  $M$  are scalars, the corresponding dimension will be squeezed out on output.

**Return type** float or array\_like

**name** = 'default'

**projected** (*cosmo, r\_t, M, a, mass\_def=None*)

Returns the 2D projected profile as a function of cosmology, radius, halo mass and scale factor.

$$\Sigma(R) = \int dr_{\parallel} \rho(\sqrt{r_{\parallel}^2 + R^2})$$

#### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **r** (*float or array\_like*) – comoving radius in Mpc.
- **M** (*float or array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **mass\_def** (*MassDef*) – a mass definition object.

**Returns** halo profile. The shape of the output will be  $(N_M, N_r)$  where  $N_r$  and  $N_m$  are the sizes of  $r$  and  $M$  respectively. If  $r$  or  $M$  are scalars, the corresponding dimension will be squeezed out on output.

**Return type** float or array\_like

**real** (*cosmo, r, M, a, mass\_def=None*)

Returns the 3D real-space value of the profile as a function of cosmology, radius, halo mass and scale factor.

#### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **r** (*float or array\_like*) – comoving radius in Mpc.

- **M** (*float* or *array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **mass\_def** (*MassDef*) – a mass definition object.

**Returns** halo profile. The shape of the output will be  $(N_M, N_r)$  where  $N_r$  and  $N_m$  are the sizes of  $r$  and  $M$  respectively. If  $r$  or  $M$  are scalars, the corresponding dimension will be squeezed out on output.

**Return type** *float* or *array\_like*

**update\_precision\_ffolog** (*\*\*kwargs*)

Update any of the precision parameters used by FFTLog to compute Hankel transforms. The available parameters are:

#### Parameters

- **padding\_lo\_ffolog** (*float*) – when computing a Hankel transform we often need to extend the range of the input (e.g. the  $r$ -range for the real-space profile when computing the Fourier-space one) to avoid aliasing and boundary effects. This parameter controls the factor by which we multiply the lower end of the range (e.g. a value of 0.1 implies that we will extend the range by one decade on the left). Note that FFTLog works in logarithmic space. Default value: 0.1.
- **padding\_hi\_ffolog** (*float*) – same as *padding\_lo\_ffolog* for the upper end of the range (e.g. a value of 10 implies extending the range by one decade on the right). Default value: 10.
- **n\_per\_decade** (*float*) – number of samples of the profile taken per decade when computing Hankel transforms.
- **padding\_lo\_extra** (*float*) – when computing the projected 2D profile or the 2D cumulative density, sometimes two Hankel transforms are needed (from 3D real-space to Fourier, then from Fourier to 2D real-space). This parameter controls the  $k$  range of the intermediate transform. The logic here is to avoid the range twice by *padding\_lo\_ffolog* (which can be overkill and slow down the calculation). Default value: 0.1.
- **padding\_hi\_extra** (*float*) – same as *padding\_lo\_extra* for the upper end of the range. Default value: 10. **large\_padding\_2D** (*bool*): if set to *True*, the intermediate Hankel transform in the calculation of the 2D projected profile and cumulative mass density will use *padding\_lo\_ffolog* and *padding\_hi\_ffolog* instead of *padding\_lo\_extra* and *padding\_hi\_extra* to extend the range of the intermediate Hankel transform.
- **extrapol** (*string*) – type of extrapolation used in the uncommon scenario that FFTLog returns a profile on a range that does not cover the intended output range. Pass *linx\_liny* if you want to extrapolate linearly in the profile and *linx\_logy* if you want to extrapolate linearly in its logarithm. Default value: *linx\_liny*.
- **plaw\_fourier** (*float*) – FFTLog is able to perform more accurate Hankel transforms by prewhitening its arguments (essentially making them flatter over the range of integration to avoid aliasing). This parameter corresponds to a guess of what the tilt of the profile is (i.e.  $\text{profile}(r) = r^{\text{tilt}}$ ), which FFTLog uses to prewhiten it. This parameter is used when computing the real  $\leftrightarrow$  Fourier transforms. The methods *\_get\_plaw\_fourier* allows finer control over this parameter. The default value allows for a slightly faster (but potentially less accurate) FFTLog transform. Some level of experimentation with this parameter is recommended when implementing a new profile. Default value: -1.5.
- **plaw\_projected** (*float*) – same as *plaw\_fourier* for the calculation of the 2D projected and cumulative density profiles. Finer control can be achieved with the *\_get\_plaw\_projected*. The default value allows for a slightly faster (but potentially less

accurate) FFTLog transform. Some level of experimentation with this parameter is recommended when implementing a new profile. Default value: -1.

**class** `pyccl.halos.profiles.HaloProfileEinasto` (*c\_M\_relation*, *truncated=True*)

Bases: `pyccl.halos.profiles.HaloProfile`

Einasto profile (1965TrAlm...5...87E).

$$\rho(r) = \rho_0 \exp(-2((r/r_s)^\alpha - 1)/\alpha)$$

where  $r_s$  is related to the spherical overdensity halo radius  $R_\Delta(M)$  through the concentration parameter  $c(M)$  as

$$R_\Delta(M) = c(M) r_s$$

and the normalization  $\rho_0$  is the mean density within the  $R_\Delta(M)$  of the halo. The index  $\alpha$  depends on halo mass and redshift, and we use the parameterization of Diemer & Kravtsov (arXiv:1401.1216).

By default, this profile is truncated at  $r = R_\Delta(M)$ .

#### Parameters

- **c\_M\_relation** (Concentration) – concentration-mass relation to use with this profile.
- **truncated** (*bool*) – set to *True* if the profile should be truncated at  $r = R_\Delta$  (i.e. zero at larger radii).

**name** = 'Einasto'

**class** `pyccl.halos.profiles.HaloProfileGaussian` (*r\_scale*, *rho0*)

Bases: `pyccl.halos.profiles.HaloProfile`

Gaussian profile

$$\rho(r) = \rho_0 e^{-(r/r_s)^2}$$

#### Parameters

- **r\_scale** (function) – the width of the profile. The signature of this function should be  $f(\text{cosmo}, M, a, mdef)$ , where *cosmo* is a `Cosmology` object, *M* is a halo mass in units of  $M_\text{sun}$ , *a* is the scale factor and *mdef* is a `MassDef` object.
- **rho0** (function) – the amplitude of the profile. It should have the same signature as *r\_scale*.

**name** = 'Gaussian'

**class** `pyccl.halos.profiles.HaloProfileHOD` (*c\_M\_relation*, *lMmin\_0=12.0*, *lMmin\_p=0.0*,  
*siglM\_0=0.4*, *siglM\_p=0.0*, *lM0\_0=7.0*,  
*lM0\_p=0.0*, *lM1\_0=13.3*, *lM1\_p=0.0*,  
*alpha\_0=1.0*, *alpha\_p=0.0*, *fc\_0=1.0*,  
*fc\_p=0.0*, *bg\_0=1.0*, *bg\_p=0.0*, *bmax\_0=1.0*,  
*bmax\_p=0.0*, *a\_pivot=1.0*)

Bases: `pyccl.halos.profiles.HaloProfile`

A generic halo occupation distribution (HOD) profile describing the number density of galaxies as a function of halo mass.

The parametrization for the mean profile is:

$$\langle n_g(r) | M, a \rangle = \bar{N}_c(M, a) [f_c(a) + \bar{N}_s(M, a) u_{\text{sat}}(r | M, a)]$$



where  $\bar{N}_c$  and  $\bar{N}_s$  are the mean number of central and satellite galaxies respectively,  $f_c$  is the observed fraction of central galaxies, and  $u_{\text{sat}}(r|M, a)$  is the distribution of satellites as a function of distance to the halo centre.

These quantities are parametrized as follows:

$$\bar{N}_c(M, a) = \frac{1}{2} \left[ 1 + \operatorname{erf} \left( \frac{\log(M/M_{\min})}{\sigma_{\ln M}} \right) \right]$$

$$\bar{N}_s(M, a) = \Theta(M - M_0) \left( \frac{M - M_0}{M_1} \right)^\alpha$$

$$u_s(r|M, a) \propto \frac{\Theta(r_{\max} - r)}{(r/r_g)(1 + r/r_g)^2}$$

Where  $\Theta(x)$  is the Heaviside step function, and the proportionality constant in the last equation is such that the volume integral of  $u_s$  is 1. The radius  $r_g$  is related to the NFW scale radius  $r_s$  through  $r_g = \beta_g r_s$ , and the radius  $r_{\max}$  is related to the overdensity radius  $r_\Delta$  as  $r_{\max} = \beta_{\max} r_\Delta$ . The scale radius is related to the comoving overdensity halo radius via  $R_\Delta(M) = c(M) r_s$ .

All the quantities  $\log_{10} M_{\min}$ ,  $\log_{10} M_0$ ,  $\log_{10} M_1$ ,  $\sigma_{\ln M}$ ,  $f_c$ ,  $\alpha$ ,  $\beta_g$  and  $\beta_{\max}$  are time-dependent via a linear expansion around a pivot scale factor  $a_*$  with an offset ( $X_0$ ) and a tilt parameter ( $X_p$ ):

$$X(a) = X_0 + X_p (a - a_*).$$

This definition of the HOD profile draws from several papers in the literature, including: astro-ph/0408564, arXiv:1706.05422 and arXiv:1912.08209. The default values used here are roughly compatible with those found in the latter paper.

See *Profile2ptHOD* for a description of the Fourier-space two-point correlator of the HOD profile.

### Parameters

- **c\_M\_relation** (Concentration) – concentration-mass relation to use with this profile.
- **lMmin\_0** (*float*) – offset parameter for  $\log_{10} M_{\min}$ .
- **lMmin\_p** (*float*) – tilt parameter for  $\log_{10} M_{\min}$ .
- **siglM\_0** (*float*) – offset parameter for  $\sigma_{\ln M}$ .
- **siglM\_p** (*float*) – tilt parameter for  $\sigma_{\ln M}$ .
- **lM0\_0** (*float*) – offset parameter for  $\log_{10} M_0$ .
- **lM0\_p** (*float*) – tilt parameter for  $\log_{10} M_0$ .
- **lM1\_0** (*float*) – offset parameter for  $\log_{10} M_1$ .
- **lM1\_p** (*float*) – tilt parameter for  $\log_{10} M_1$ .
- **alpha\_0** (*float*) – offset parameter for  $\alpha$ .
- **alpha\_p** (*float*) – tilt parameter for  $\alpha$ .
- **fc\_0** (*float*) – offset parameter for  $f_c$ .
- **fc\_p** (*float*) – tilt parameter for  $f_c$ .
- **bg\_0** (*float*) – offset parameter for  $\beta_g$ .
- **bg\_p** (*float*) – tilt parameter for  $\beta_g$ .
- **bmax\_0** (*float*) – offset parameter for  $\beta_{\max}$ .
- **bmax\_p** (*float*) – tilt parameter for  $\beta_{\max}$ .

- **a\_pivot** (*float*) – pivot scale factor  $a_*$ .

**name** = 'HOD'

**update\_parameters** (*lMmin\_0=None, lMmin\_p=None, siglM\_0=None, siglM\_p=None, lM0\_0=None, lM0\_p=None, lM1\_0=None, lM1\_p=None, alpha\_0=None, alpha\_p=None, fc\_0=None, fc\_p=None, bg\_0=None, bg\_p=None, bmax\_0=None, bmax\_p=None, a\_pivot=None*)

Update any of the parameters associated with this profile. Any parameter set to *None* won't be updated.

#### Parameters

- **lMmin\_0** (*float*) – offset parameter for  $\log_{10} M_{\min}$ .
- **lMmin\_p** (*float*) – tilt parameter for  $\log_{10} M_{\min}$ .
- **siglM\_0** (*float*) – offset parameter for  $\sigma_{\ln M}$ .
- **siglM\_p** (*float*) – tilt parameter for  $\sigma_{\ln M}$ .
- **lM0\_0** (*float*) – offset parameter for  $\log_{10} M_0$ .
- **lM0\_p** (*float*) – tilt parameter for  $\log_{10} M_0$ .
- **lM1\_0** (*float*) – offset parameter for  $\log_{10} M_1$ .
- **lM1\_p** (*float*) – tilt parameter for  $\log_{10} M_1$ .
- **alpha\_0** (*float*) – offset parameter for  $\alpha$ .
- **alpha\_p** (*float*) – tilt parameter for  $\alpha$ .
- **fc\_0** (*float*) – offset parameter for  $f_c$ .
- **fc\_p** (*float*) – tilt parameter for  $f_c$ .
- **bg\_0** (*float*) – offset parameter for  $\beta_g$ .
- **bg\_p** (*float*) – tilt parameter for  $\beta_g$ .
- **bmax\_0** (*float*) – offset parameter for  $\beta_{\max}$ .
- **bmax\_p** (*float*) – tilt parameter for  $\beta_{\max}$ .
- **a\_pivot** (*float*) – pivot scale factor  $a_*$ .

**class** `pyccl.halos.profiles.HaloProfileHernquist` (*c\_M\_relation, truncated=True*)

Bases: `pyccl.halos.profiles.HaloProfile`

Hernquist (1990ApJ...356..359H).

$$\rho(r) = \frac{\rho_0}{\frac{r}{r_s} \left(1 + \frac{r}{r_s}\right)^3}$$

where  $r_s$  is related to the spherical overdensity halo radius  $R_\Delta(M)$  through the concentration parameter  $c(M)$  as

$$R_\Delta(M) = c(M) r_s$$

and the normalization  $\rho_0$  is the mean density within the  $R_\Delta(M)$  of the halo.

By default, this profile is truncated at  $r = R_\Delta(M)$ .

#### Parameters

- **c\_M\_relation** (*Concentration*) – concentration-mass relation to use with this profile.

- **truncated** (*bool*) – set to *True* if the profile should be truncated at  $r = R_\Delta$  (i.e. zero at larger radii).

`name = 'Hernquist'`

```
class pyccl.halos.profiles.HaloProfileNFW(c_M_relation,
                                         fourier_analytic=True,
                                         projected_analytic=False,
                                         cumul2d_analytic=False,
                                         truncated=True)
```

Bases: `pyccl.halos.profiles.HaloProfile`

Navarro-Frenk-White (astro-ph:astro-ph/9508025) profile.

$$\rho(r) = \frac{\rho_0}{\frac{r}{r_s} \left(1 + \frac{r}{r_s}\right)^2}$$

where  $r_s$  is related to the spherical overdensity halo radius  $R_\Delta(M)$  through the concentration parameter  $c(M)$  as

$$R_\Delta(M) = c(M) r_s$$

and the normalization  $\rho_0$  is

$$\rho_0 = \frac{M}{4\pi r_s^3 [\log(1+c) - c/(1+c)]}$$

By default, this profile is truncated at  $r = R_\Delta(M)$ .

#### Parameters

- **c\_M\_relation** (Concentration) – concentration-mass relation to use with this profile.
- **fourier\_analytic** (*bool*) – set to *True* if you want to compute the Fourier profile analytically (and not through FFTLog). Default: *False*.
- **projected\_analytic** (*bool*) – set to *True* if you want to compute the 2D projected profile analytically (and not through FFTLog). Default: *False*.
- **cumul2d\_analytic** (*bool*) – set to *True* if you want to compute the 2D cumulative surface density analytically (and not through FFTLog). Default: *False*.
- **truncated** (*bool*) – set to *True* if the profile should be truncated at  $r = R_\Delta$  (i.e. zero at larger radii).

`name = 'NFW'`

```
class pyccl.halos.profiles.HaloProfilePowerLaw(r_scale, tilt)
```

Bases: `pyccl.halos.profiles.HaloProfile`

Power-law profile

$$\rho(r) = (r/r_s)^\alpha$$

#### Parameters

- **r\_scale** (function) – the correlation length of the profile. The signature of this function should be  $f(\text{cosmo}, M, a, mdef)$ , where *cosmo* is a *Cosmology* object, *M* is a halo mass in units of  $M_{\text{sun}}$ , *a* is the scale factor and *mdef* is a *MassDef* object.
- **tilt** (function) – the power law index of the profile. The signature of this function should be  $f(\text{cosmo}, a)$ .

`name = 'PowerLaw'`

```
class pycccl.halos.profiles.HaloProfilePressureGNFW (mass_bias=0.8, P0=6.41,
                                                    c500=1.81, alpha=1.33, alpha_P=0.12,
                                                    beta=4.13,
                                                    gamma=0.31, P0_hexp=-1.0,
                                                    qrange=(0.001, 1000.0), nq=128)
```

Bases: `pycccl.halos.profiles.HaloProfile`

Generalized NFW pressure profile by Arnaud et al. (2010A&A...517A..92A).

The parametrization is:

$$P_e(r) = C \times P_0 h_{70}^E (c_{500} x)^{-\gamma} [1 + (c_{500} x)^\alpha]^{(\gamma-\beta)/\alpha},$$

where

$$C = 1.65 h_{70}^2 \left( \frac{H(z)}{H_0} \right)^{8/3} \left[ \frac{h_{70} \tilde{M}_{500}}{3 \times 10^{14} M_\odot} \right]^{2/3+0.12},$$

$x = r/\tilde{r}_{500}$ ,  $h_{70} = h/0.7$ , and the exponent  $E$  is -1 for SZ-based profile normalizations and -1.5 for X-ray-based normalizations. The biased mass  $\tilde{M}_{500}$  is related to the true overdensity mass  $M_{500}$  via the mass bias parameter  $(1 - b)$  as  $\tilde{M}_{500} = (1 - b)M_{500}$ .  $\tilde{r}_{500}$  is the overdensity halo radius associated with  $\tilde{M}_{500}$  (note the intentional tilde!), and the profile is defined for a halo overdensity  $\Delta = 500$  with respect to the critical density.

The default arguments (other than *mass\_bias*), correspond to the profile parameters used in the Planck 2013 (V) paper. The profile is calculated in physical (non-comoving) units of eV/cm<sup>3</sup>.

### Parameters

- **mass\_bias** (*float*) – the mass bias parameter  $1 - b$ .
- **P0** (*float*) – profile normalization.
- **c500** (*float*) – concentration parameter.
- **alpha** (*float*) – profile shape parameter.
- **beta** (*float*) – profile shape parameter.
- **gamma** (*float*) – profile shape parameter.
- **alpha\_P** (*float*) – additional mass dependence exponent
- **P0\_hexp** (*float*) – power of  $h$  with which the normalization parameter should scale (-1 for SZ-based normalizations, -3/2 for X-ray-based ones).
- **qrange** (*tuple*) – limits of integration to be used when precomputing the Fourier-space profile template, as fractions of the virial radius.
- **nq** (*int*) – number of points over which the Fourier-space profile template will be sampled.

**name** = 'GNFW'

**update\_parameters** (*mass\_bias*=None, *P0*=None, *c500*=None, *alpha*=None, *beta*=None, *gamma*=None, *alpha\_P*=None, *P0\_hexp*=None)

Update any of the parameters associated with this profile. Any parameter set to *None* won't be updated.

---

**Note:** A change in *alpha*, *beta* or *gamma* will trigger a recomputation of the Fourier-space template, which can be slow.

---

### Parameters

- **mass\_bias** (*float*) – the mass bias parameter  $1 - b$ .

- **P0** (*float*) – profile normalization.
- **c500** (*float*) – concentration parameter.
- **alpha** (*float*) – profile shape parameter.
- **beta** (*float*) – profile shape parameters.
- **gamma** (*float*) – profile shape parameters.
- **alpha\_P** (*float*) – additional mass dependence exponent.
- **P0\_hexp** (*float*) – power of  $h$  with which the normalization should scale (-1 for SZ-based normalizations, -3/2 for X-ray-based ones).

## pyccl.halos.profiles\_2pt module

**class** pyccl.halos.profiles\_2pt.**Profile2pt**

Bases: `object`

This class implements the 1-halo 2-point correlator between two halo profiles. In the simplest case, this is just the product of both profiles in Fourier space. More complicated cases should be implemented by subclassing this class and overloading the `fourier_2pt()` method.

**fourier\_2pt** (*prof, cosmo, k, M, a, prof2=None, mass\_def=None*)

Returns the Fourier-space two-point moment between two profiles:

$$\langle \rho_1(k) \rho_2(k) \rangle.$$

### Parameters

- **prof** (*HaloProfile*) – halo profile for which the second-order moment is desired.
- **cosmo** (*Cosmology*) – a Cosmology object.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **M** (*float or array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **prof2** (*HaloProfile*) – second halo profile for which the second-order moment is desired. If *None*, the assumption is that you want an auto-correlation, and *prof* will be used as *prof2*.
- **mass\_def** (*MassDef*) – a mass definition object.

**Returns** second-order Fourier-space moment. The shape of the output will be  $(N_M, N_k)$  where  $N_k$  and  $N_m$  are the sizes of  $k$  and  $M$  respectively. If  $k$  or  $M$  are scalars, the corresponding dimension will be squeezed out on output.

**Return type** `float` or `array_like`

**class** pyccl.halos.profiles\_2pt.**Profile2ptHOD**

Bases: `pyccl.halos.profiles_2pt.Profile2pt`

This class implements the Fourier-space 1-halo 2-point correlator for the HOD profile.

$$\langle n_g^2(k) | M, a \rangle = \bar{N}_c(M, a) [2f_c(a)\bar{N}_s(M, a)u_{\text{sat}}(r|M, a) + (\bar{N}_s(M, a)u_{\text{sat}}(r|M, a))^2],$$

where all quantities are described in the documentation of `HaloProfileHOD`.

**fourier\_2pt** (*prof, cosmo, k, M, a, prof2=None, mass\_def=None*)

Returns the Fourier-space two-point moment for the HOD profile.

### Parameters

- **prof** (*HaloProfileHOD*) – halo profile for which the second-order moment is desired.
- **cosmo** (*Cosmology*) – a Cosmology object.
- **k** (*float or array\_like*) – comoving wavenumber in  $\text{Mpc}^{-1}$ .
- **M** (*float or array\_like*) – halo mass in units of  $M_{\text{sun}}$ .
- **a** (*float*) – scale factor.
- **prof2** (*HaloProfile*) – second halo profile for which the second-order moment is desired. If *None*, the assumption is that you want an auto-correlation. Note that only auto-correlations are allowed in this case.
- **mass\_def** (*MassDef*) – a mass definition object.

**Returns** second-order Fourier-space moment. The shape of the output will be  $(N_M, N_k)$  where  $N_k$  and  $N_m$  are the sizes of  $k$  and  $M$  respectively. If  $k$  or  $M$  are scalars, the corresponding dimension will be squeezed out on output.

**Return type** `float` or `array_like`

## Module contents

### pyccl.nl\_pt package

### Submodules

### pyccl.nl\_pt.power module

```
class pyccl.nl_pt.power.PTCalculator (with_NC=False, with_IA=False, with_dd=True,  
log10k_min=-4, log10k_max=2, nk_per_decade=20,  
pad_factor=1, low_extrap=-5, high_extrap=3,  
P_window=None, C_window=0.75)
```

Bases: `object`

This class implements a set of methods that can be used to compute the various components needed to estimate perturbation theory correlations. These calculations are currently based on FAST-PT (<https://github.com/JoeMcEwen/FAST-PT>).

### Parameters

- **with\_NC** (*bool*) – set to True if you’ll want to use this calculator to compute correlations involving number counts.
- **with\_IA** (*bool*) – set to True if you’ll want to use this calculator to compute correlations involving intrinsic alignments.
- **with\_dd** (*bool*) – set to True if you’ll want to use this calculator to compute the one-loop matter power spectrum.
- **log10k\_min** (*float*) – decimal logarithm of the minimum Fourier scale (in  $\text{Mpc}^{-1}$ ) for which you want to calculate perturbation theory quantities.
- **log10k\_max** (*float*) – decimal logarithm of the maximum Fourier scale (in  $\text{Mpc}^{-1}$ ) for which you want to calculate perturbation theory quantities.
- **pad\_factor** (*float*) – fraction of the  $\log(k)$  interval you want to add as padding for FFTLog calculations within FAST-PT.

- **low\_extrap** (*float*) – decimal logarithm of the minimum Fourier scale (in  $\text{Mpc}^{-1}$ ) for which FAST-PT will extrapolate.
- **high\_extrap** (*float*) – decimal logarithm of the maximum Fourier scale (in  $\text{Mpc}^{-1}$ ) for which FAST-PT will extrapolate.
- **P\_window** (*array\_like or None*) – 2-element array describing the tapering window used by FAST-PT. See FAST-PT documentation for more details.
- **C\_window** (*float*) – *C\_window* parameter used by FAST-PT to smooth the edges and avoid ringing. See FAST-PT documentation for more details.

**get\_pgg** (*Pd1d1, g4, b11, b21, bs1, b12, b22, bs2, sub\_lowk*)

Get the number counts auto-spectrum at the internal set of wavenumbers (given by this object's *ks* attribute) and a number of redshift values.

#### Parameters

- **Pd1d1** (*array\_like*) – 1-loop matter power spectrum at the wavenumber values given by this object's *ks* list.
- **g4** (*array\_like*) – fourth power of the growth factor at a number of redshifts.
- **b11** (*array\_like*) – 1-st order bias for the first tracer being correlated at the same set of input redshifts.
- **b21** (*array\_like*) – 2-nd order bias for the first tracer being correlated at the same set of input redshifts.
- **bs1** (*array\_like*) – tidal bias for the first tracer being correlated at the same set of input redshifts.
- **b12** (*array\_like*) – 1-st order bias for the second tracer being correlated at the same set of input redshifts.
- **b22** (*array\_like*) – 2-nd order bias for the second tracer being correlated at the same set of input redshifts.
- **bs2** (*array\_like*) – tidal bias for the second tracer being correlated at the same set of input redshifts.
- **sub\_lowk** (*bool*) – if True, the small-scale white noise contribution will be subtracted.

**Returns** 2D array of shape  $(N_k, N_z)$ , where  $N_k$  is the size of this object's *ks* attribute, and  $N_z$  is the size of the input redshift-dependent biases and growth factor.

**Return type** *array\_like*

**get\_pgi** (*Pd1d1, g4, b1, b2, bs, c1, c2, cd*)

Get the number counts - IA cross-spectrum at the internal set of wavenumbers (given by this object's *ks* attribute) and a number of redshift values.

---

**Note:** The full non-linear model for the cross-correlation between number counts and intrinsic alignments is still work in progress in FastPT. As a workaround CCL assumes a non-linear treatment of IAs, but only linearly biased number counts.

---

#### Parameters

- **Pd1d1** (*array\_like*) – 1-loop matter power spectrum at the wavenumber values given by this object's *ks* list.
- **g4** (*array\_like*) – fourth power of the growth factor at a number of redshifts.

- **b1** (*array\_like*) – 1-st order bias for the number counts being correlated at the same set of input redshifts.
- **b2** (*array\_like*) – 2-nd order bias for the number counts being correlated at the same set of input redshifts.
- **bs** (*array\_like*) – tidal bias for the number counts being correlated at the same set of input redshifts.
- **c1** (*array\_like*) – 1-st order bias for the IA tracer being correlated at the same set of input redshifts.
- **c2** (*array\_like*) – 2-nd order bias for the IA tracer being correlated at the same set of input redshifts.
- **cd** (*array\_like*) – overdensity bias for the IA tracer being correlated at the same set of input redshifts.

**Returns** 2D array of shape  $(N_k, N_z)$ , where  $N_k$  is the size of this object’s *ks* attribute, and  $N_z$  is the size of the input redshift-dependent biases and growth factor.

**Return type** *array\_like*

**get\_pgm** (*Pd1d1, g4, b1, b2, bs*)

Get the number counts - matter cross-spectrum at the internal set of wavenumbers (given by this object’s *ks* attribute) and a number of redshift values.

**Parameters**

- **Pd1d1** (*array\_like*) – 1-loop matter power spectrum at the wavenumber values given by this object’s *ks* list.
- **g4** (*array\_like*) – fourth power of the growth factor at a number of redshifts.
- **b1** (*array\_like*) – 1-st order bias for the number counts tracer being correlated at the same set of input redshifts.
- **b2** (*array\_like*) – 2-nd order bias for the number counts tracer being correlated at the same set of input redshifts.
- **bs** (*array\_like*) – tidal bias for the number counts tracer being correlated at the same set of input redshifts.

**Returns** 2D array of shape  $(N_k, N_z)$ , where  $N_k$  is the size of this object’s *ks* attribute, and  $N_z$  is the size of the input redshift-dependent biases and growth factor.

**Return type** *array\_like*

**get\_pii** (*Pd1d1, g4, c11, c21, cd1, c12, c22, cd2, return\_bb=False, return\_both=False*)

Get the intrinsic alignment auto-spectrum at the internal set of wavenumbers (given by this object’s *ks* attribute) and a number of redshift values.

**Parameters**

- **Pd1d1** (*array\_like*) – 1-loop matter power spectrum at the wavenumber values given by this object’s *ks* list.
- **g4** (*array\_like*) – fourth power of the growth factor at a number of redshifts.
- **c11** (*array\_like*) – 1-st order bias for the first tracer being correlated at the same set of input redshifts.
- **c21** (*array\_like*) – 2-nd order bias for the first tracer being correlated at the same set of input redshifts.



- **cd1** (*array\_like*) – overdensity bias for the first tracer being correlated at the same set of input redshifts.
- **c12** (*array\_like*) – 1-st order bias for the second tracer being correlated at the same set of input redshifts.
- **c22** (*array\_like*) – 2-nd order bias for the second tracer being correlated at the same set of input redshifts.
- **cd2** (*array\_like*) – overdensity bias for the second tracer being correlated at the same set of input redshifts.
- **return\_bb** (*bool*) – if *True*, the B-mode power spectrum will be returned.
- **return\_both** (*bool*) – if *True*, both the E- and B-mode power spectra will be returned. Supersedes *return\_bb*.

**Returns** 2D array of shape  $(N_k, N_z)$ , where  $N_k$  is the size of this object’s *ks* attribute, and  $N_z$  is the size of the input redshift-dependent biases and growth factor.

**Return type** *array\_like*

**get\_pim** (*Pd1d1*, *g4*, *c1*, *c2*, *cd*)

Get the intrinsic alignment - matter cross-spectrum at the internal set of wavenumbers (given by this object’s *ks* attribute) and a number of redshift values.

**Parameters**

- **Pd1d1** (*array\_like*) – 1-loop matter power spectrum at the wavenumber values given by this object’s *ks* list.
- **g4** (*array\_like*) – fourth power of the growth factor at a number of redshifts.
- **c1** (*array\_like*) – 1-st order bias for the IA tracer being correlated at the same set of input redshifts.
- **c2** (*array\_like*) – 2-nd order bias for the IA tracer being correlated at the same set of input redshifts.
- **cd** (*array\_like*) – overdensity bias for the IA tracer being correlated at the same set of input redshifts.

**Returns** 2D array of shape  $(N_k, N_z)$ , where  $N_k$  is the size of this object’s *ks* attribute, and  $N_z$  is the size of the input redshift-dependent biases and growth factor.

**Return type** *array\_like*

**get\_pmm** (*Pd1d1\_lin*, *g4*)

Get the one-loop matter power spectrum.

**Parameters**

- **Pd1d1\_lin** (*array\_like*) – 1-loop linear matter power spectrum at the wavenumber values given by this object’s *ks* list.
- **g4** (*array\_like*) – fourth power of the growth factor at a number of redshifts.

**Returns** 2D array of shape  $(N_k, N_z)$ , where  $N_k$  is the size of this object’s *ks* attribute, and  $N_z$  is the size of the input redshift-dependent biases and growth factor.

**Return type** *array\_like*

**update\_pk** (*pk*)

Update the internal PT arrays.

**Parameters** `pk` (*array\_like*) – linear power spectrum sampled at the internal  $k$  values used by this calculator.

```
pyccl.nl_pt.power.get_pt_pk2d(cosmo, tracer1, tracer2=None, ptc=None, sub_lowk=False,
                              nonlin_pk_type='nonlinear', a_arr=None,
                              extrap_order_lok=1, extrap_order_hik=2, return_ia_bb=False,
                              return_ia_ee_and_bb=False)
```

Returns a *Pk2D* object containing the PT power spectrum for two quantities defined by two *PTTracer* objects.

---

**Note:** The full non-linear model for the cross-correlation between number counts and intrinsic alignments is still work in progress in FastPT. As a workaround CCL assumes a non-linear treatment of IAs, but only linearly biased number counts.

---

### Parameters

- **cosmo** (*Cosmology*) – a Cosmology object.
- **tracer1** (*PTTracer*) – the first tracer being correlated.
- **ptc** (*PTCalculator*) – a perturbation theory calculator.
- **tracer2** (*PTTracer*) – the second tracer being correlated. If *None*, the auto-correlation of the first tracer will be returned.
- **sub\_lowk** (*bool*) – if *True*, the small-scale white noise contribution will be subtracted for number counts auto-correlations.
- **nonlin\_pk\_type** (*str*) – type of 1-loop matter power spectrum to use. ‘linear’ for linear  $P(k)$ , ‘nonlinear’ for the internal non-linear power spectrum, ‘spt’ for standard perturbation theory power spectrum. Default: ‘nonlinear’.
- **a\_arr** (*array*) – an array holding values of the scale factor at which the power spectrum should be calculated for interpolation. If *None*, the internal values used by *cosmo* will be used.
- **extrap\_order\_lok** (*int*) – extrapolation order to be used on  $k$ -values below the minimum of the splines. See *Pk2D*.
- **extrap\_order\_hik** (*int*) – extrapolation order to be used on  $k$ -values above the maximum of the splines. See *Pk2D*.
- **return\_ia\_bb** (*bool*) – if *True*, the B-mode power spectrum for intrinsic alignments will be returned (if both input tracers are of type *PTIntrinsicAlignmentTracer*) If *False* (default) E-mode power spectrum is returned.
- **return\_ia\_ee\_and\_bb** (*bool*) – if *True*, the E-mode power spectrum for intrinsic alignments will be returned in addition to the B-mode one (if both input tracers are of type *PTIntrinsicAlignmentTracer*) If *False* (default) E-mode power spectrum is returned. Supersedes *return\_ia\_bb*.

**Returns** PT power spectrum.

**Return type** *Pk2D*

### pyccl.nl\_pt.tracers module

```
class pyccl.nl_pt.tracers.PTIntrinsicAlignmentTracer(c1, c2=None, cdelta=None)
    Bases: pyccl.nl_pt.tracers.PTTracer
```

*PTTracer* representing intrinsic alignments. This is described by 1st and 2nd-order alignment biases and an overdensity bias. These are provided as floating point numbers or tuples of (reshift,bias) arrays. If a number is provided, a constant bias is assumed. If *None*, a bias of zero is assumed.

#### Parameters

- **c1** (*float or tuple of arrays*) – a single number or a tuple of arrays (z, c1(z)) giving the first-order alignment bias.
- **c2** (*float or tuple of arrays*) – as above for the second-order alignment bias.
- **cdelta** (*float or tuple of arrays*) – as above for the overdensity bias.

**c1**

Internal first-order bias function.

**c2**

Internal second-order bias function.

**cdelta**

Internal overdensity bias function.

**class** `pyccl.nl_pt.tracers.PTMatterTracer`

Bases: `pyccl.nl_pt.tracers.PTTracer`

*PTTracer* representing matter fluctuations.

**class** `pyccl.nl_pt.tracers.PTNumberCountsTracer` (*b1, b2=None, bs=None*)

Bases: `pyccl.nl_pt.tracers.PTTracer`

*PTTracer* representing number count fluctuations. This is described by 1st and 2nd-order biases and a tidal field bias. These are provided as floating point numbers or tuples of (reshift,bias) arrays. If a number is provided, a constant bias is assumed. If *None*, a bias of zero is assumed.

#### Parameters

- **b1** (*float or tuple of arrays*) – a single number or a tuple of arrays (z, b(z)) giving the first-order bias.
- **b2** (*float or tuple of arrays*) – as above for the second-order bias.
- **bs** (*float or tuple of arrays*) – as above for the tidal bias.

**b1**

Internal first-order bias function.

**b2**

Internal second-order bias function.

**bs**

Internal tidal bias function.

**class** `pyccl.nl_pt.tracers.PTTracer`

Bases: `object`

*PTTracers* contain the information necessary to describe the perturbative, non-linear inhomogeneities associated with different physical quantities.

In essence their main function is to store a set of redshift- dependent functions (e.g. perturbation theory biases) needed in a perturbation theory framework to provide N-point correlations.

**get\_bias** (*bias\_name, z*)

Get the value of one of the bias functions at a given redshift.

#### Parameters

- **bias\_name** (*str*) – name of the bias function to return.
- **z** (*float or array\_like*) – redshift.

**Returns** bias value at the input redshifts.

**Return type** *float* or *array\_like*

`pyccl.nl_pt.tracers.translate_IA_norm(cosmo, z, a1=1.0, a1delta=None, a2=None, Om_m2_for_c2=False, Om_m_fid=0.3)`

Function to convert from *a\_ia* values to *c\_ia* values, using the standard convention of Blazek 2019 or the variant used by the Dark Energy Survey analysis.

**Parameters**

- **cosmo** (*Cosmology*) – cosmology object.
- **z** (*float or array\_like*) – z value(s) where amplitude is evaluated
- **a1** (*float or array\_like*) – IA a1 at input z values. Defaults to 1.0
- **a1delta** (*float or array\_like*) – IA a1delta at input z values. Defaults to None.
- **a2** (*float or array\_like*) – IA a2 at input z values. Defaults to None.
- **Om\_m2\_for\_c2** (*bool*) – True to use the Blazek 2019 convention of  $\text{Om}_m^2$  scaling. Defaults to False
- **Om\_m\_fid** (*float*) – Value for Blazek 2019 scaling. Defaults to 0.3.

**Returns** IA c1 at input z values c1delta (*float or array\_like*): IA c1delta at input z values c2 (*float or array\_like*): IA c2 at input z values

**Return type** *c1* (*float or array\_like*)

**Module contents**

**14.1.2 Submodules**

**pyccl.background module**

Smooth background quantities

CCL defines seven species types:

- ‘matter’: cold dark matter and baryons
- ‘dark\_energy’: cosmological constant or otherwise
- ‘radiation’: relativistic species besides massless neutrinos (i.e., only photons)
- ‘curvature’: curvature density
- ‘neutrinos\_rel’: relativistic neutrinos
- ‘neutrinos\_massive’: massive neutrinos

These strings define the *species* inputs to the functions below.

`pyccl.background.Sig_MG(cosmo, a)`

Redshift-dependent modification to Poisson equation for massless particles under modified gravity.

**Parameters**

- **cosmo** (*Cosmology*) – a Cosmology object.

- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Modification to Poisson equation under modified gravity at scale factor *a*. *Sig\_MG* is assumed to be proportional to *Omega\_Lambda(z)*, see e.g. Abbott et al. 2018, 1810.02499, Eq. 9.

**Return type** *float* or *array\_like*

`pyccl.background.angular_diameter_distance` (*cosmo*, *a1*, *a2=None*)  
Angular diameter distance.

---

**Note:** The angular diameter distance in Mpc from scale factor *a1* to scale factor *a2*. If *a2* is not provided, it is assumed that the distance will be calculated between 1 and *a1*. Note that *a2* has to be smaller than *a1*.

---

#### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a1** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.
- **a2** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today,
- **optional.** –

**Returns** angular diameter distance; Mpc.

**Return type** *float* or *array\_like*

`pyccl.background.comoving_angular_distance` (*cosmo*, *a*)  
Comoving angular distance.

---

**Note:** This quantity is otherwise known as the transverse comoving distance, and is NOT angular diameter distance or angular separation. The comoving angular distance is defined such that the comoving distance between two objects at a fixed scale factor separated by an angle  $\theta$  is  $\theta r_A(a)$  where  $r_A(a)$  is the comoving angular distance.

---

#### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Comoving angular distance; Mpc.

**Return type** *float* or *array\_like*

`pyccl.background.comoving_radial_distance` (*cosmo*, *a*)  
Comoving radial distance.

#### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Comoving radial distance; Mpc.

**Return type** *float* or *array\_like*

`pyccl.background.distance_modulus` (*cosmo*, *a*)  
Distance Modulus, defined as  $5 * \log_{10}(\text{luminosity distance} / 10 \text{ pc})$ .

---

**Note:** The distance modulus can be used to convert between apparent and absolute magnitudes via  $m = M + \text{distance modulus}$ , where  $m$  is the apparent magnitude and  $M$  is the absolute magnitude.

---

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Distance modulus at *a*.

**Return type** *float* or *array\_like*

`pyccl.background.growth_factor` (*cosmo*, *a*)  
Growth factor.

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Growth factor, normalized to unity today.

**Return type** *float* or *array\_like*

`pyccl.background.growth_factor_unnorm` (*cosmo*, *a*)  
Unnormalized growth factor.

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Unnormalized growth factor, normalized to the scale factor at early times.

**Return type** *float* or *array\_like*

`pyccl.background.growth_rate` (*cosmo*, *a*)  
Growth rate defined as the logarithmic derivative of the growth factor,  $d \ln D / d \ln a$ .

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Growth rate.

**Return type** *float* or *array\_like*

`pyccl.background.h_over_h0` (*cosmo*, *a*)  
Ratio of Hubble constant at *a* over Hubble constant today.

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns**  $H(a)/H_0$ .

**Return type** float or array\_like

`pyccl.background.luminosity_distance` (*cosmo*, *a*)  
Luminosity distance.

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float or array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Luminosity distance; Mpc.

**Return type** float or array\_like

`pyccl.background.mu_MG` (*cosmo*, *a*)  
Redshift-dependent modification to Poisson equation under modified gravity.

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float or array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Modification to Poisson equation under modified gravity at a scale factor. `mu_MG` is assumed to be proportional to `Omega_Lambda(z)`, see e.g. Abbott et al. 2018, 1810.02499, Eq. 9.

**Return type** float or array\_like

`pyccl.background.omega_x` (*cosmo*, *a*, *species*)  
Density fraction of a given species at a redshift different than  $z=0$ .

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float or array\_like*) – Scale factor(s), normalized to 1 today.
- **species** (*string*) – species type. Should be one of
  - 'matter': cold dark matter, massive neutrinos, and baryons
  - 'dark\_energy': cosmological constant or otherwise
  - 'radiation': relativistic species besides massless neutrinos
  - 'curvature': curvature density
  - 'neutrinos\_rel': relativistic neutrinos
  - 'neutrinos\_massive': massive neutrinos

**Returns** Density fraction of a given species at a scale factor.

**Return type** float or array\_like

`pyccl.background.rho_x` (*cosmo*, *a*, *species*, *is\_comoving=False*)  
Physical or comoving density as a function of scale factor.

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float or array\_like*) – Scale factor(s), normalized to 1 today.
- **species** (*string*) – species type. Should be one of
  - 'matter': cold dark matter, massive neutrinos, and baryons

- ‘dark\_energy’: cosmological constant or otherwise
- ‘radiation’: relativistic species besides massless neutrinos
- ‘curvature’: curvature density
- ‘neutrinos\_rel’: relativistic neutrinos
- ‘neutrinos\_massive’: massive neutrinos
- **is\_comoving** (*bool*) – either physical (False, default) or comoving (True)

**Returns** Physical density of a given species at a scale factor.

**Return type** *rho\_x* (*float* or *array\_like*)

`pyccl.background.scale_factor_of_chi` (*cosmo, chi*)

Scale factor, *a*, at a comoving radial distance *chi*.

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **chi** (*float* or *array\_like*) – Comoving radial distance(s); Mpc.

**Returns** Scale factor(s), normalized to 1 today.

**Return type** *float* or *array\_like*

## pyccl.bcm module

`pyccl.bcm.bcm_model_fka` (*cosmo, k, a*)

The BCM model correction factor for baryons.

---

**Note:** BCM stands for the “baryonic correction model” of Schneider & Teyssier (2015; <https://arxiv.org/abs/1510.06034>). See the [DESC Note](#) for details.

---

---

**Note:** The correction factor is applied multiplicatively so that  $P_{\text{corrected}}(k, a) = P(k, a) f_{\text{bcm}}(k, a)$ .

---

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **k** (*float* or *array\_like*) – Wavenumber;  $\text{Mpc}^{-1}$ .
- **a** (*float*) – Scale factor.

**Returns** Correction factor to apply to the power spectrum.

**Return type** *float* or *array\_like*

## pyccl.boltzmann module

`pyccl.boltzmann.get_camb_pk_lin` (*cosmo*)

Run CAMB and return the linear power spectrum.

**Parameters** **cosmo** (*Cosmology*) – Cosmological parameters. The cosmological parameters with which to run CAMB.

**Returns** Power spectrum object. The linear power spectrum.



**Return type** *Pk2D*

`pyccl.boltzmann.get_class_pk_lin(cosmo)`

Run CLASS and return the linear power spectrum.

**Parameters** `cosmo` (*Cosmology*) – Cosmological parameters. The cosmological parameters with which to run CLASS.

**Returns** Power spectrum object. The linear power spectrum.

**Return type** *Pk2D*

`pyccl.boltzmann.get_isitgr_pk_lin(cosmo)`

Run ISiTGR-CAMB and return the linear power spectrum.

**Parameters** `cosmo` (*Cosmology*) – Cosmological parameters. The cosmological parameters with which to run ISiTGR-CAMB.

**Returns** Power spectrum object. The linear power spectrum.

**Return type** *Pk2D*

## pyccl.cls module

`pyccl.cls.angular_cl(cosmo, cltracer1, cltracer2, ell, p_of_k_a=None, l_limber=-1.0, limber_integration_method='qag_quad')`

Calculate the angular (cross-)power spectrum for a pair of tracers.

**Parameters**

- `cosmo` (*Cosmology*) – A Cosmology object.
- `cltracer1` (*Tracer*) – a *Tracer* object, of any kind.
- `cltracer2` (*Tracer*) – a second *Tracer* object, of any kind.
- `ell` (*float* or *array\_like*) – Angular wavenumber(s) at which to evaluate the angular power spectrum.
- `p_of_k_a` (*Pk2D* or *None*) – 3D Power spectrum to project. If *None*, the non-linear matter power spectrum will be used.
- `l_limber` (*float*) – Angular wavenumber beyond which Limber’s approximation will be used. Defaults to -1.
- `limber_integration_method` (*string*) – integration method to be used for the Limber integrals. Possibilities: ‘qag\_quad’ (GSL’s *qag* method backed up by *quad* when it fails) and ‘spline’ (the integrand is splined and then integrated analytically).

**Returns** Angular (cross-)power spectrum values,  $C_\ell$ , for the pair of tracers, as a function of  $\ell$ .

**Return type** *float* or *array\_like*

## pyccl.core module

The core functionality of ccl, including the core data types. This includes the cosmology and parameters objects used to instantiate a model from which one can compute a set of theoretical predictions.

```
class pyccl.core.Cosmology (Omega_c=None, Omega_b=None, h=None, n_s=None,
sigma8=None, A_s=None, Omega_k=0.0, Omega_g=None,
Neff=3.046, m_nu=0.0, m_nu_type=None, w0=-1.0, wa=0.0,
T_CMB=None, bcm_log10Mc=14.079181246047625,
bcm_etab=0.5, bcm_ks=55.0, mu_0=0.0,
sigma_0=0.0, z_mg=None, df_mg=None, trans-
fer_function='boltzmann_camb', matter_power_spectrum='halofit',
baryons_power_spectrum='nobaryons', mass_function='tinker10',
halo_concentration='duffy2008', emulator_neutrinos='strict')
```

Bases: `object`

A cosmology including parameters and associated data.

---

**Note:** Although some arguments default to *None*, they will raise a `ValueError` inside this function if not specified, so they are not optional.

---

---

**Note:** The parameter `Omega_g` can be used to set the radiation density (not including relativistic neutrinos) to zero. Doing this will give you a model that is physically inconsistent since the temperature of the CMB will still be non-zero. Note however that this approximation is common for late-time LSS computations.

---

---

**Note:** BCM stands for the “baryonic correction model” of Schneider & Teyssier (2015; <https://arxiv.org/abs/1510.06034>). See the [DESC Note](#) for details.

---

---

**Note:** After instantiation, you can set parameters related to the internal splines and numerical integration accuracy by setting the values of the attributes of `Cosmology.cosmo.spline_params` and `Cosmology.cosmo.gsl_params`. For example, you can set the generic relative accuracy for integration by executing `c = Cosmology(...); c.cosmo.gsl_params.INTEGRATION_EPSREL = 1e-5`. See the module level documetaion of `pyccl.core` for details.

---

### Parameters

- **Omega\_c** (`float`) – Cold dark matter density fraction.
- **Omega\_b** (`float`) – Baryonic matter density fraction.
- **h** (`float`) – Hubble constant divided by 100 km/s/Mpc; unitless.
- **A\_s** (`float`) – Power spectrum normalization. Exactly one of `A_s` and `sigma_8` is required.
- **sigma8** (`float`) – Variance of matter density perturbations at an 8 Mpc/h scale. Exactly one of `A_s` and `sigma_8` is required.
- **n\_s** (`float`) – Primordial scalar perturbation spectral index.
- **Omega\_k** (`float`, optional) – Curvature density fraction. Defaults to 0.
- **Omega\_g** (`float`, optional) – Density in relativistic species except massless neutrinos. The default of *None* corresponds to setting this from the CMB temperature. Note that if a non-*None* value is given, this may result in a physically inconsistent model because the CMB temperature will still be non-zero in the parameters.

- **Neff** (`float`, optional) – Effective number of massless neutrinos present. Defaults to 3.046.
- **m\_nu** (`float`, optional) – Total mass in eV of the massive neutrinos present. Defaults to 0.
- **m\_nu\_type** (`str`, optional) – The type of massive neutrinos. Should be one of ‘inverted’, ‘normal’, ‘equal’, ‘single’, or ‘list’. The default of None is the same as ‘normal’.
- **w0** (`float`, optional) – First order term of dark energy equation of state. Defaults to -1.
- **wa** (`float`, optional) – Second order term of dark energy equation of state. Defaults to 0.
- **T\_CMB** (`float`) – The CMB temperature today. The default of None uses the global CCL value in `pyccl.physical_constants.T_CMB`.
- **bcm\_log10Mc** (`float`, optional) – One of the parameters of the BCM model. Defaults to  $np.log10(1.2e14)$ .
- **bcm\_etab** (`float`, optional) – One of the parameters of the BCM model. Defaults to 0.5.
- **bcm\_ks** (`float`, optional) – One of the parameters of the BCM model. Defaults to 55.0.
- **mu\_0** (`float`, optional) – One of the parameters of the mu-Sigma modified gravity model. Defaults to 0.0
- **sigma\_0** (`float`, optional) – One of the parameters of the mu-Sigma modified gravity model. Defaults to 0.0
- **df\_mg** (`array_like`, *optional*) – Perturbations to the GR growth rate as a function of redshift  $\Delta f$ . Used to implement simple modified growth scenarios.
- **z\_mg** (`array_like`, *optional*) – Array of redshifts corresponding to `df_mg`.
- **transfer\_function** (`str`, optional) – The transfer function to use. Defaults to ‘boltzmann\_camb’.
- **matter\_power\_spectrum** (`str`, optional) – The matter power spectrum to use. Defaults to ‘halofit’.
- **baryons\_power\_spectrum** (`str`, optional) – The correction from baryonic effects to be implemented. Defaults to ‘nobaryons’.
- **mass\_function** (`str`, optional) – The mass function to use. Defaults to ‘tinker10’ (2010).
- **halo\_concentration** (`str`, optional) – The halo concentration relation to use. Defaults to Duffy et al. (2008) ‘duffy2008’.
- **emulator\_neutrinos** – *str*, optional): If using the emulator for the power spectrum, specified treatment of unequal neutrinos. Options are ‘strict’, which will raise an error and quit if the user fails to pass either a set of three equal masses or a sum with `m_nu_type = ‘equal’`, and ‘equalize’, which will redistribute masses to be equal right before calling the emulator but results in internal inconsistencies. Defaults to ‘strict’.

**compute\_distances** ()

Compute the distance splines.

**compute\_growth** ()

Compute the growth function.

**compute\_linear\_power** ()

Call the appropriate function to compute the linear power spectrum, either read from input or calculated internally,

**compute\_nonlin\_power** ()

Call the appropriate function to compute the linear power spectrum, either read from input or calculated internally,

**compute\_sigma** ()

Compute the  $\sigma(M)$  and mass function splines.

**has\_distances**

Checks if the distances have been precomputed.

**has\_growth**

Checks if the growth function has been precomputed.

**has\_linear\_power**

Checks if the linear power spectra have been precomputed.

**has\_nonlin\_power**

Checks if the non-linear power spectra have been precomputed.

**has\_sigma**

Checks if  $\sigma(M)$  is precomputed.

**classmethod read\_yaml** (*filename*)

Read the parameters from a YAML file.

**Parameters** *filename* (*str*) –

**status** ()

Get error status of the `ccl_cosmology` object.

---

**Note:** The error statuses are currently under development and may not be fully descriptive.

---

**Returns** *str* containing the status message.

**write\_yaml** (*filename*)

Write a YAML representation of the parameters to file.

**Parameters** *filename* (*str*) –

**class** `pyccl.core.CosmologyVanillaLCDM` (\*\**kwargs*)

Bases: `pyccl.core.Cosmology`

A cosmology with typical flat Lambda-CDM parameters ( $\Omega_c=0.25$ ,  $\Omega_b = 0.05$ ,  $\Omega_k = 0$ ,  $\sigma_8 = 0.81$ ,  $n_s = 0.96$ ,  $h = 0.67$ , no massive neutrinos).

**Parameters** **\*\*kwargs** (*dict*) – a dictionary of parameters passed as arguments to the *Cosmology* constructor. It should not contain any of the LambdaCDM parameters (“ $\Omega_c$ ”, “ $\Omega_b$ ”, “ $n_s$ ”, “ $\sigma_8$ ”, “ $A_s$ ”, “ $h$ ”), since these are fixed.

## pyccl.correlation module

Correlation function computations.

**Choices of algorithms used to compute correlation functions:** ‘Bessel’ is a direct integration using Bessel functions. ‘FFTLog’ is fast using a fast Fourier transform. ‘Legendre’ uses a sum over Legendre polynomials.

`pyccl.correlation.correlation` (*cosmo*, *ell*, *C\_ell*, *theta*, *type*='NN', *corr\_type*=None, *method*='fftlog')

Compute the angular correlation function.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **ell** (*array\_like*) – Multipoles corresponding to the input angular power spectrum.
- **C\_ell** (*array\_like*) – Input angular power spectrum.
- **theta** (*float or array\_like*) – Angular separation(s) at which to calculate the angular correlation function (in degrees).
- **type** (*string*) – Type of correlation function. Choices: ‘NN’ (0x0), ‘NG’ (0x2), ‘GG+’ (2x2, xi+), ‘GG-’ (2x2, xi-), where numbers refer to the spins of the two quantities being cross-correlated (see Section 2.4.2 of the CCL paper).
- **method** (*string, optional*) – Method to compute the correlation function. Choices: ‘Bessel’ (direct integration over Bessel function), ‘FFTLog’ (fast integration with FFTLog), ‘Legendre’ (brute-force sum over Legendre polynomials).
- **corr\_type** (*string*) – (deprecated, please use *type*) Type of correlation function. Choices: ‘gg’ (0x0), ‘gl’ (0x2), ‘l+’ (2x2, xi+), ‘l-’ (2x2, xi-), where the numbers refer to the spins of the two quantities being cross-correlated (see Section 2.4.2 of the CCL paper).

**Returns** Value(s) of the correlation function at the input angular separations.

**Return type** *float* or *array\_like*

`pyccl.correlation.correlation_3d` (*cosmo, a, r*)  
Compute the 3D correlation function.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **a** (*float*) – scale factor.
- **r** (*float or array\_like*) – distance(s) at which to calculate the 3D correlation function (in Mpc).

**Returns** Value(s) of the correlation function at the input distance(s).

`pyccl.correlation.correlation_3dRsd` (*cosmo, a, s, mu, beta, use\_spline=True*)  
Compute the 3DRsd correlation function using linear approximation with multipoles.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **a** (*float*) – scale factor.
- **s** (*float or array\_like*) – distance(s) at which to calculate the 3DRsd correlation function (in Mpc).
- **mu** (*float*) – cosine of the angle at which to calculate the 3DRsd correlation function (in Radian).
- **beta** (*float*) – growth rate divided by galaxy bias.
- **use\_spline** – switch that determines whether the RSD correlation function is calculated using global splines of multipoles.

**Returns** Value(s) of the correlation function at the input distance(s) & angle.

`pyccl.correlation.correlation_3dRsd_avgmu` (*cosmo, a, s, beta*)  
Compute the 3DRsd correlation function averaged over mu at constant s.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **a** (*float*) – scale factor.
- **s** (*float or array\_like*) – distance(s) at which to calculate the 3DRsd correlation function (in Mpc).
- **beta** (*float*) – growth rate divided by galaxy bias.

**Returns** Value(s) of the correlation function at the input distance(s) & angle.

`pyccl.correlation.correlation_multipole` (*cosmo, a, beta, l, s*)  
Compute the correlation multipoles.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **a** (*float*) – scale factor.
- **beta** (*float*) – growth rate divided by galaxy bias.
- **l** (*int*) – the desired multipole
- **s** (*float or array\_like*) – distance(s) at which to calculate the 3DRsd correlation function (in Mpc).

**Returns** Value(s) of the correlation function at the input distance(s).

`pyccl.correlation.correlation_pi_sigma` (*cosmo, a, beta, pi, sig, use\_spline=True*)  
Compute the 3DRsd correlation in pi-sigma space.

**Parameters**

- **cosmo** (*Cosmology*) – A Cosmology object.
- **a** (*float*) – scale factor.
- **pi** (*float*) – distance times cosine of the angle (in Mpc).
- **sig** (*float or array-like*) – distance(s) times sine of the angle (in Mpc).
- **beta** (*float*) – growth rate divided by galaxy bias.

**Returns** Value(s) of the correlation function at the input pi and sigma.

## pyccl.errors module

**exception** `pyccl.errors.CCLError`

Bases: `RuntimeError`

A CCL-specific `RuntimeError`

**exception** `pyccl.errors.CCLWarning`

Bases: `RuntimeWarning`

A CCL-specific warning

## pyccl.halomodel module

`pyccl.halomodel.halo_concentration` (*cosmo, halo\_mass, a, odelta=200*)

Halo mass concentration relation

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **halo\_mass** (*float or array\_like*) – Halo masses; Msun.
- **a** (*float*) – scale factor.
- **odelta** (*float*) – overdensity parameter (default: 200)

**Returns** Dimensionless halo concentration, ratio  $r_v/r_s$

**Return type** *float* or *array\_like*

`pyccl.halomodel.halomodel_matter_power(cosmo, k, a)`

Matter power spectrum from halo model assuming NFW density profiles

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **k** (*float or array\_like*) – wavenumber
- **a** (*float*) – scale factor.

**Returns** matter power spectrum from halo model

**Return type** *float* or *array\_like*

`pyccl.halomodel.onehalo_matter_power(cosmo, k, a)`

One-halo term for matter power spectrum assuming NFW density profiles

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **k** (*float or array\_like*) – wavenumber
- **a** (*float*) – scale factor.

**Returns** one-halo term for matter power spectrum

**Return type** *float* or *array\_like*

`pyccl.halomodel.twohalo_matter_power(cosmo, k, a)`

Two-halo term for matter power spectrum assuming NFW density profiles

**Parameters**

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **k** (*float or array\_like*) – wavenumber
- **a** (*float*) – scale factor.

**Returns** two-halo term for matter power spectrum.

**Return type** *float* or *array\_like*

## pyccl.haloprofile module

`pyccl.haloprofile.einasto_profile_3d(cosmo, concentration, halo_mass, odelta, a, r)`

Calculate the 3D Einasto halo profile at a given radius or an array of radii, for a halo with a given mass, mass definition, and concentration, at a given scale factor, with a cosmology dependence. The alpha parameter is calibrated using the relation with peak height in <https://arxiv.org/pdf/1401.1216.pdf> eqn5, assuming virial mass.

---

**Note:** Note that this function is deprecated. Please use the functionality in the *profiles* module.

---

**Parameters**

- **cosmo** (*Cosmology*) – cosmological parameters.
- **concentration** (*float*) – halo concentration.
- **halo\_mass** (*float*) – halo masses; in units of Msun.
- **odelta** (*float*) – overdensity with respect to mean matter density.
- **a** (*float*) – scale factor.
- **r** (*float or array\_like*) – radius or radii to calculate profile for, in units of Mpc.

**Returns** 3D NFW density at r, in units of Msun/Mpc<sup>3</sup>.

**Return type** *float* or *array\_like*

`pyccl.haloprofile.hernquist_profile_3d(cosmo, concentration, halo_mass, odelta, a, r)`

Calculate the 3D Hernquist halo profile at a given radius or an array of radii, for a halo with a given mass, mass definition, and concentration, at a given scale factor, with a cosmology dependence.

---

**Note:** Note that this function is deprecated. Please use the functionality in the *profiles* module.

---

**Parameters**

- **cosmo** (*Cosmology*) – cosmological parameters.
- **concentration** (*float*) – halo concentration.
- **halo\_mass** (*float*) – halo masses; in units of Msun.
- **odelta** (*float*) – overdensity with respect to mean matter density.
- **a** (*float*) – scale factor.
- **r** (*float or array\_like*) – radius or radii to calculate profile for, in units of Mpc.

**Returns** 3D NFW density at r, in units of Msun/Mpc<sup>3</sup>.

**Return type** *float* or *array\_like*

`pyccl.haloprofile.nfw_profile_2d(cosmo, concentration, halo_mass, odelta, a, r)`

Calculate the 2D projected NFW halo profile at a given radius or an array of radii, for a halo with a given mass, mass definition, and concentration, at a given scale factor, with a cosmology dependence.

---

**Note:** Note that this function is deprecated. Please use the functionality in the *profiles* module.

---

**Parameters**

- **cosmo** (*Cosmology*) – cosmological parameters.
- **concentration** (*float*) – halo concentration.
- **halo\_mass** (*float*) – halo masses; in units of Msun.
- **odelta** (*float*) – overdensity with respect to mean matter density.
- **a** (*float*) – scale factor.
- **r** (*float or array\_like*) – radius or radii to calculate profile for, in units of Mpc.



**Returns** 2D projected NFW density at  $r$ , in units of  $M_{\text{sun}}/\text{Mpc}^2$ .

**Return type** `float` or `array_like`

`pyccl.haloprofile.nfw_profile_3d(cosmo, concentration, halo_mass, odelta, a, r)`

Calculate the 3D NFW halo profile at a given radius or an array of radii, for a halo with a given mass, mass definition, and concentration, at a given scale factor, with a cosmology dependence.

---

**Note:** Note that this function is deprecated. Please use the functionality in the `profiles` module.

---

#### Parameters

- **cosmo** (*Cosmology*) – cosmological parameters.
- **concentration** (*float*) – halo concentration.
- **halo\_mass** (*float*) – halo masses; in units of  $M_{\text{sun}}$ .
- **odelta** (*float*) – overdensity with respect to mean matter density.
- **a** (*float*) – scale factor.
- **r** (*float or array\_like*) – radius or radii to calculate profile for, in units of  $\text{Mpc}$ .

**Returns** 3D NFW density at  $r$ , in units of  $M_{\text{sun}}/\text{Mpc}^3$ .

**Return type** `float` or `array_like`

### pyccl.massfunction module

`pyccl.massfunction.halo_bias(cosmo, halo_mass, a, overdensity=200)`

Halo bias

---

**Note:** Note that this function is deprecated. Please use the functionality in the `hbias` module.

---

#### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **halo\_mass** (*float or array\_like*) – Halo masses;  $M_{\text{sun}}$ .
- **a** (*float*) – Scale factor.
- **overdensity** (*float*) – Overdensity parameter (default: 200).

**Returns** Halo bias.

**Return type** `float` or `array_like`

`pyccl.massfunction.massfunc(cosmo, halo_mass, a, overdensity=200)`

Halo mass function,  $dn/d\log_{10}M$ .

---

**Note:** Note that this function is deprecated. Please use the functionality in the `hmfunc` module.

---

#### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.

- **halo\_mass** (*float or array\_like*) – Halo masses; Msun.
- **a** (*float*) – scale factor.
- **overdensity** (*float*) – overdensity parameter (default: 200)

**Returns** Halo mass function; dn/dlog10M.

**Return type** *float* or *array\_like*

`pyccl.massfunction.massfunc_m2r` (*cosmo, halo\_mass*)  
Converts smoothing halo mass into smoothing halo radius.

---

**Note:** This is  $R = (3M/(4\pi\rho_M))^{1/3}$ , where  $\rho_M$  is the mean comoving matter density.

---

---

**Note:** Note that this function is deprecated. Please use `mass2radius_lagrangian()`.

---

#### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **halo\_mass** (*float or array\_like*) – Halo masses; Msun.

**Returns** Smoothing halo radius; Mpc.

**Return type** *float* or *array\_like*

### pyccl.neutrinos module

`pyccl.neutrinos.Omeganh2` (*a, m\_nu, T\_CMB=None*)  
Calculate  $\Omega_\nu h^2$  at a given scale factor given the neutrino masses.

#### Parameters

- **a** (*float or array-like*) – Scale factor, normalized to 1 today.
- **m\_nu** (*float or array-like*) – Neutrino mass(es) (in eV)
- **T\_CMB** (*float, optional*) – Temperature of the CMB (K). Default: 2.725.

**Returns**  $\Omega_\nu h^2$  at a given scale factor given the neutrino masses

**Return type** *float* or *array\_like*

`pyccl.neutrinos.nu_masses` (*OmNuh2, mass\_split, T\_CMB=None*)  
Returns the neutrinos mass(es) for a given OmNuh2, according to the splitting convention specified by the user.

#### Parameters

- **OmNuh2** (*float*) – Neutrino energy density at z=0 times h<sup>2</sup>
- **mass\_split** (*str*) – indicates how the masses should be split up Should be one of ‘normal’, ‘inverted’, ‘equal’ or ‘sum’.
- **T\_CMB** (*float, optional*) – Temperature of the CMB (K). Default: 2.725.

**Returns** Neutrino mass(es) corresponding to this Omeganh2

**Return type** *float* or *array-like*

**pyccl.pk2d module**

**class** `pyccl.pk2d.Pk2D` (*pkfunc=None, a\_arr=None, lk\_arr=None, pk\_arr=None, is\_logp=True, extrap\_order\_lok=1, extrap\_order\_hik=2, cosmo=None*)

Bases: `object`

A power spectrum class holding the information needed to reconstruct an arbitrary function of wavenumber and scale factor.

**Parameters**

- **pkfunc** (*function*) – a function returning a floating point number or numpy array with the signature  $f(k,a)$ , where  $k$  is a wavenumber (in units of  $\text{Mpc}^{-1}$ ) and  $a$  is the scale factor. The function must be able to take numpy arrays as  $k$ . The function must return the value(s) of the power spectrum (or its natural logarithm, depending on the value of *is\_logp*). The power spectrum units should be compatible with those used by CCL (e.g. if you're passing a matter power spectrum, its units should be  $\text{Mpc}^3$ ). If this argument is not *None*, this function will be sampled at the values of  $k$  and  $a$  used internally by CCL to store the linear and non-linear power spectra.
- **a\_arr** (*array*) – an array holding values of the scale factor
- **lk\_arr** (*array*) – an array holding values of the natural logarithm of the wavenumber (in units of  $\text{Mpc}^{-1}$ ).
- **pk\_arr** (*array*) – a 2D array containing the values of the power spectrum at the values of the scale factor and the wavenumber held by *a\_arr* and *lk\_arr*. The shape of this array must be  $[na, nk]$ , where *na* is the size of *a\_arr* and *nk* is the size of *lk\_arr*. This array can be provided in a flattened form as long as the total size matches  $nk*na$ . The array can hold the values of the natural logarithm of the power spectrum, depending on the value of *is\_logp*. If *pkfunc* is not *None*, then *a\_arr*, *lk\_arr* and *pk\_arr* are ignored. However, either *pkfunc* or all of the last three arrays must be non-*None*. Note that, if you pass your own Pk array, you are responsible of making sure that it is sufficiently well sampled (i.e. the resolution of *a\_arr* and *lk\_arr* is high enough to sample the main features in the power spectrum). For reference, CCL will use bicubic interpolation to evaluate the power spectrum at any intermediate point in  $k$  and  $a$ .
- **extrap\_order\_lok** (*int*) – extrapolation order to be used on  $k$ -values below the minimum of the splines (use 0, 1 or 2). Note that the extrapolation will be done in either  $\log(P(k))$  or  $P(k)$ , depending on the value of *is\_logp*.
- **extrap\_order\_hik** (*int*) – extrapolation order to be used on  $k$ -values above the maximum of the splines (use 0, 1 or 2). Note that the extrapolation will be done in either  $\log(P(k))$  or  $P(k)$ , depending on the value of *is\_logp*.
- **is\_logp** (*boolean*) – if *True*, *pkfunc*/*pkarr* return/hold the natural logarithm of the power spectrum. Otherwise, the true value of the power spectrum is expected. Note that arrays will be interpolated in log space if *is\_logp* is set to *True*.
- **cosmo** (*Cosmology*) – Cosmology object. The cosmology object is needed in order if *pkfunc* is not *None*. The object is used to determine the sampling rate in scale factor and wavenumber.

**eval** (*k, a, cosmo*)

Evaluate power spectrum.

**Parameters**

- **k** (*float or array\_like*) – wavenumber value(s) in units of  $\text{Mpc}^{-1}$ .
- **a** (*float*) – value of the scale factor

- **cosmo** (*Cosmology*) – Cosmology object. The cosmology object is needed in order to evaluate the power spectrum outside the interpolation range in *a*. E.g. if you want to evaluate the power spectrum at a very small *a*, not covered by the arrays you passed when initializing this object, the power spectrum will be extrapolated from the earliest available value using the linear growth factor (for which a cosmology is needed).
- **a\_arr** (*array*) – an array holding values of the scale factor.

**Returns** value(s) of the power spectrum.

**Return type** `float` or `array_like`

## pyccl.power module

`pyccl.power.kNL` (*cosmo, a*)  
Scale for the non-linear cut.

---

**Note:** `k_NL` is calculated based on Lagrangian perturbation theory as the inverse of the variance of the displacement field, i.e.  $k_{NL} = 1/\sigma_{\eta} = [1/(6 \pi^2) * \int P_L(k) dk]^{-1/2}$ .

---

### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **a** (*float* or *array\_like*) – Scale factor(s), normalized to 1 today.

**Returns** Scale of non-linear cut-off;  $\text{Mpc}^{-1}$ .

**Return type** `float` or `array-like`

`pyccl.power.linear_matter_power` (*cosmo, k, a*)  
The linear matter power spectrum;  $\text{Mpc}^3$ .

### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **k** (*float* or *array\_like*) – Wavenumber;  $\text{Mpc}^{-1}$ .
- **a** (*float*) – Scale factor.

**Returns** Linear matter power spectrum;  $\text{Mpc}^3$ .

**Return type** `float` or `array_like`

`pyccl.power.nonlin_matter_power` (*cosmo, k, a*)  
The nonlinear matter power spectrum;  $\text{Mpc}^3$ .

### Parameters

- **cosmo** (*Cosmology*) – Cosmological parameters.
- **k** (*float* or *array\_like*) – Wavenumber;  $\text{Mpc}^{-1}$ .
- **a** (*float*) – Scale factor.

**Returns** Nonlinear matter power spectrum;  $\text{Mpc}^3$ .

**Return type** `float` or `array_like`

`pyccl.power.sigma8(cosmo)`  
RMS variance in a top-hat sphere of radius 8 Mpc/h.

---

**Note:** 8 Mpc/h is rescaled based on the chosen value of the Hubble constant within *cosmo*.

---

**Parameters** `cosmo` (*Cosmology*) – Cosmological parameters.

**Returns** RMS variance in top-hat sphere of radius 8 Mpc/h.

**Return type** `float`

`pyccl.power.sigmaM(cosmo, M, a)`  
Root mean squared variance for the given halo mass of the linear power spectrum; Msun.

**Parameters**

- `cosmo` (*Cosmology*) – Cosmological parameters.
- `M` (*float or array\_like*) – Halo masses; Msun.
- `a` (*float*) – scale factor.

**Returns** RMS variance of halo mass.

**Return type** `float` or `array_like`

`pyccl.power.sigmaR(cosmo, R, a=1.0)`  
RMS variance in a top-hat sphere of radius R in Mpc.

**Parameters**

- `cosmo` (*Cosmology*) – Cosmological parameters.
- `R` (*float or array\_like*) – Radius; Mpc.
- `a` (*float*) – optional scale factor; defaults to `a=1`

**Returns** RMS variance in the density field in top-hat sphere; Mpc.

**Return type** `float` or `array_like`

`pyccl.power.sigmaV(cosmo, R, a=1.0)`  
RMS variance in the displacement field in a top-hat sphere of radius R. The linear displacement field is the gradient of the linear density field.

**Parameters**

- `cosmo` (*Cosmology*) – Cosmological parameters.
- `R` (*float or array\_like*) – Radius; Mpc.
- `a` (*float*) – optional scale factor; defaults to `a=1`

**Returns** RMS variance in the displacement field in top-hat sphere.

**Return type** `sigmaV` (`float` or `array_like`)

## pyccl.pyutils module

Utility functions to analyze status and error messages passed from CCL, as well as wrappers to automatically vectorize functions.

`pyccl.pyutils.assert_warns` (*wtype, f, \*args, \*\*kwargs*)

Check that a function call `f(*args, **kwargs)` raises a warning of type `wtype`.

Returns the output of `f(*args, **kwargs)` unless there was no warning, in which case an `AssertionError` is raised.

`pyccl.pyutils.check` (*status, cosmo=None*)

Check the status returned by a `ccllib` function.

**Parameters**

- **status** (*int* or *error\_types*) – Flag or error describing the success of a function.
- **cosmo** (*Cosmology*, optional) – A `Cosmology` object.

`pyccl.pyutils.debug_mode` (*debug*)

Toggle debug mode on or off. If debug mode is on, the C backend is forced to print error messages as soon as they are raised, even if the flow of the program continues. This makes it easier to track down errors.

If debug mode is off, the C code will not print errors, and the Python wrapper will raise the last error that was detected. If multiple errors were raised, all but the last will be overwritten within the C code, so the user will not necessarily be informed of the root cause of the error.

**Parameters** **debug** (*bool*) – Switch debug mode on (True) or off (False).

`pyccl.pyutils.deprecated` (*new\_function=None*)

This is a decorator which can be used to mark functions as deprecated. It will result in a warning being emitted when the function is used. If there is a replacement function, pass it as *new\_function*.

`pyccl.pyutils.resample_array` (*x\_in, y\_in, x\_out, extrap\_lo='none', extrap\_hi='none', fill\_value\_lo=0, fill\_value\_hi=0*)

Interpolates an input `y` array onto a set of `x` values.

**Parameters**

- **x\_in** (*array\_like*) – input `x`-values.
- **y\_in** (*array\_like*) – input `y`-values.
- **x\_out** (*array\_like*) – `x`-values for output array.
- **extrap\_lo** (*string*) – type of extrapolation for `x`-values below the range of `x_in`. ‘none’ (for no interpolation), ‘constant’, ‘linx\_liny’ (linear in `x` and `y`), ‘linx\_logy’, ‘logx\_liny’ and ‘logx\_logy’.
- **extrap\_hi** (*string*) – type of extrapolation for `x`-values above the range of `x_in`.
- **fill\_value\_lo** (*float*) – constant value if `extrap_lo` is ‘constant’.
- **fill\_value\_hi** (*float*) – constant value if `extrap_hi` is ‘constant’.

**Returns** output array.

**Return type** `array_like`

**pyccl.tracers module**

**class** `pyccl.tracers.CMBLensingTracer` (*cosmo, z\_source, n\_samples=100*)

Bases: `pyccl.tracers.Tracer`

A Tracer for CMB lensing.

**Parameters**

- **cosmo** (*Cosmology*) – `Cosmology` object.

- **z\_source** (*float*) – Redshift of source plane for CMB lensing.
- **nsamples** (*int, optional*) – number of samples over which the kernel is desired. These will be equi-spaced in radial distance. The kernel is quite smooth, so usually O(100) samples is enough.

**class** `pyccl.tracers.NumberCountsTracer` (*cosmo, has\_rsd, dndz, bias, mag\_bias=None*)

Bases: `pyccl.tracers.Tracer`

Specific *Tracer* associated to galaxy clustering with linear scale-independent bias, including redshift-space distortions and magnification.

#### Parameters

- **cosmo** (*Cosmology*) – Cosmology object.
- **has\_rsd** (*bool*) – Flag for whether the tracer has a redshift-space distortion term.
- **dndz** (*tuple of arrays*) – A tuple of arrays (*z, N(z)*) giving the redshift distribution of the objects. The units are arbitrary; *N(z)* will be normalized to unity.
- **bias** (*tuple of arrays*) – A tuple of arrays (*z, b(z)*) giving the galaxy bias. If *None*, this tracer won't include a term proportional to the matter density contrast.
- **mag\_bias** (*tuple of arrays, optional*) – A tuple of arrays (*z, s(z)*) giving the magnification bias as a function of redshift. If *None*, the tracer is assumed to not have magnification bias terms. Defaults to *None*.

**class** `pyccl.tracers.Tracer`

Bases: `object`

Tracers contain the information necessary to describe the contribution of a given sky observable to its cross-power spectrum with any other tracer. Tracers are composed of 4 main ingredients:

- A radial kernel: this expresses the support in redshift/distance over which this tracer extends.
- A transfer function: this is a function of wavenumber and scale factor that describes the connection between the tracer and the power spectrum on different scales and at different cosmic times.
- An ell-dependent prefactor: normally associated with angular derivatives of a given fundamental quantity.
- The order of the derivative of the Bessel functions with which they enter the computation of the angular power spectrum.

A *Tracer* object will in reality be a list of different such tracers that get combined linearly when computing power spectra. Further details can be found in Section 4.9 of the CCL note.

**add\_tracer** (*cosmo, kernel=None, transfer\_ka=None, transfer\_k=None, transfer\_a=None, der\_bessel=0, der\_angles=0, is\_logt=False, extrap\_order\_lok=0, extrap\_order\_hik=2*)  
Adds one more tracer to the list contained in this *Tracer*.

#### Parameters

- **cosmo** (*Cosmology*) – cosmology object.
- **kernel** (*tuple of arrays, optional*) – A tuple of arrays (*chi, w\_chi*) describing the radial kernel of this tracer. *chi* should contain values of the comoving radial distance in increasing order, and *w\_chi* should contain the values of the kernel at those values of the radial distance. The kernel will be assumed to be zero outside the range of distances covered by *chi*. If *kernel* is *None* a constant kernel  $w(\chi)=1$  will be assumed everywhere.
- **transfer\_ka** (*tuple of arrays, optional*) – a tuple of arrays (*a, 'lk', 't\_ka'*) describing the most general transfer function for a tracer. *a* should be an array of scale factor values in increasing order. *lk* should be an array of values of the natural logarithm of the wave number (in units of inverse Mpc) in increasing order. *t\_ka* should be an array

of shape  $(na, nk)$ , where  $na$  and  $nk$  are the sizes of  $a$  and  $lk$  respectively.  $t_{ka}$  should hold the values of the transfer function at the corresponding values of  $a$  and  $lk$ . If your transfer function is factorizable (i.e.  $T(a,k) = A(a) * K(k)$ ), it is more efficient to set this to *None* and use *transfer\_k* and *transfer\_a* to describe  $K$  and  $A$  respectively. The transfer function will be assumed continuous and constant outside the range of scale factors covered by  $a$ . It will be extrapolated using polynomials of order *extrap\_order\_lok* and *extrap\_order\_hik* below and above the range of wavenumbers covered by  $lk$  respectively. If this argument is not *None*, the values of *transfer\_k* and *transfer\_a* will be ignored.

- **transfer\_k** (*tuple of arrays, optional*) – a tuple of arrays ( $lk, 't_k'$ ) describing the scale-dependent part of a factorizable transfer function.  $lk$  should be an array of values of the natural logarithm of the wave number (in units of inverse Mpc) in increasing order.  $t_k$  should be an array of the same size holding the values of the  $k$ -dependent part of the transfer function at those wavenumbers. It will be extrapolated using polynomials of order *extrap\_order\_lok* and *extrap\_order\_hik* below and above the range of wavenumbers covered by  $lk$  respectively. If *None*, the  $k$ -dependent part of the transfer function will be set to 1 everywhere.
- **transfer\_a** (*tuple of arrays, optional*) – a tuple of arrays ( $a, 't_a'$ ) describing the time-dependent part of a factorizable transfer function.  $a$  should be an array of scale factor values in increasing order.  $t_a$  should contain the time-dependent part of the transfer function at those values of the scale factor. The time dependence will be assumed continuous and constant outside the range covered by  $a$ . If *None*, the time-dependent part of the transfer function will be set to 1 everywhere.
- **der\_bessel** (*int*) – order of the derivative of the Bessel functions with which this tracer enters the calculation of the power spectrum. Allowed values are -1, 0, 1 and 2. 0, 1 and 2 correspond to the raw functions, their first derivatives or their second derivatives. -1 corresponds to the raw functions divided by the square of their argument. We enable this special value because this type of dependence is ubiquitous for many common tracers (lensing, IAs), and makes the corresponding transfer functions more stable for small  $k$  or  $\chi$ .
- **der\_angles** (*int*) – integer describing the ell-dependent prefactor associated with this tracer. Allowed values are 0, 1 and 2. 0 means no prefactor. 1 means a prefactor  $\ell*(\ell+1)$ , associated with the angular laplacian and used e.g. for lensing convergence and magnification. 2 means a prefactor  $\sqrt{(\ell+2)!/(\ell-2)!}$ , associated with the angular derivatives of spin-2 fields (e.g. cosmic shear, IAs).
- **is\_logt** (*bool*) – if *True*, *transfer\_ka*, *transfer\_k* and *transfer\_a* will contain the natural logarithm of the transfer function (or their factorizable parts). Default is *False*.
- **extrap\_order\_lok** (*int*) – polynomial order used to extrapolate the transfer functions for low wavenumbers not covered by the input arrays.
- **extrap\_order\_hik** (*int*) – polynomial order used to extrapolate the transfer functions for high wavenumbers not covered by the input arrays.

#### **get\_bessel\_derivative** ()

Get Bessel function derivative orders for all tracers contained in this *Tracer*.

**Returns** list of Bessel derivative orders for each tracer.

**Return type** array\_like

#### **get\_dndz** (z)

Get the redshift distribution for this tracer. Only available for some tracers (*NumberCountsTracer* and *WeakLensingTracer*).

**Parameters**  $z$  (*float or array\_like*) – redshift values.



**Returns** redshift distribution evaluated at the input values of  $z$ .

**Return type** `array_like`

**get\_f\_ell** (*ell*)

Get the ell-dependent prefactors for all tracers contained in this *Tracer*.

**Parameters** **ell** (*float or array\_like*) – angular multipole values.

**Returns** list of prefactors for each tracer. The shape will be  $(n\_tracer, ell.size)$ , where  $n\_tracer$  is the number of tracers. The last dimension will be squeezed if the input is a scalar.

**Return type** `array_like`

**get\_kernel** (*chi*)

Get the radial kernels for all tracers contained in this *Tracer*.

**Parameters** **chi** (*float or array\_like*) – values of the comoving radial distance in increasing order and in Mpc.

**Returns** list of radial kernels for each tracer. The shape will be  $(n\_tracer, chi.size)$ , where  $n\_tracer$  is the number of tracers. The last dimension will be squeezed if the input is a scalar.

**Return type** `array_like`

**get\_transfer** (*lk, a*)

Get the transfer functions for all tracers contained in this *Tracer*.

**Parameters**

- **lk** (*float or array\_like*) – values of the natural logarithm of the wave number (in units of inverse Mpc) in increasing order.
- **a** (*float or array\_like*) – values of the scale factor.

**Returns** list of transfer functions for each tracer. The shape will be  $(n\_tracer, lk.size, a.size)$ , where  $n\_tracer$  is the number of tracers. The other dimensions will be squeezed if the inputs are scalars.

**Return type** `array_like`

**class** `pyccl.tracers.WeakLensingTracer` (*cosmo, dndz, has\_shear=True, ia\_bias=None, use\_A\_ia=True*)

Bases: `pyccl.tracers.Tracer`

Specific *Tracer* associated to galaxy shape distortions including lensing shear and intrinsic alignments within the L-NLA model.

**Parameters**

- **cosmo** (*Cosmology*) – Cosmology object.
- **dndz** (*tuple of arrays*) – A tuple of arrays  $(z, N(z))$  giving the redshift distribution of the objects. The units are arbitrary;  $N(z)$  will be normalized to unity.
- **has\_shear** (*bool*) – set to *False* if you want to omit the lensing shear contribution from this tracer.
- **ia\_bias** (*tuple of arrays, optional*) – A tuple of arrays  $(z, A_{IA}(z))$  giving the intrinsic alignment amplitude  $A_{IA}(z)$ . If *None*, the tracer is assumed to not have intrinsic alignments. Defaults to *None*.
- **use\_A\_ia** (*bool*) – set to *True* to use the conventional IA normalization. Set to *False* to use the raw input amplitude, which will usually be 1 for use with PT IA modeling. Defaults to *True*.

`pyccl.tracers.get_density_kernel` (*cosmo, dndz*)

This convenience function returns the radial kernel for galaxy-clustering-like tracers. Given an unnormalized redshift distribution, it returns two arrays: `chi`, `w(chi)`, where `chi` is an array of radial distances in units of Mpc and `w(chi) = p(z) * H(z)`, where `H(z)` is the expansion rate in units of  $\text{Mpc}^{-1}$  and `p(z)` is the normalized redshift distribution.

#### Parameters

- **cosmo** (*Cosmology*) – cosmology object used to transform redshifts into distances.
- **dndz** (*tuple of arrays*) – A tuple of arrays (`z`, `N(z)`) giving the redshift distribution of the objects. The units are arbitrary; `N(z)` will be normalized to unity.

`pyccl.tracers.get_kappa_kernel` (*cosmo, z\_source, nsamples*)

This convenience function returns the radial kernel for CMB-lensing-like tracers.

#### Parameters

- **cosmo** (*Cosmology*) – Cosmology object.
- **z\_source** (*float*) – Redshift of source plane for CMB lensing.
- **nsamples** (*int*) – number of samples over which the kernel is desired. These will be equi-spaced in radial distance. The kernel is quite smooth, so usually  $O(100)$  samples is enough.

`pyccl.tracers.get_lensing_kernel` (*cosmo, dndz, mag\_bias=None*)

This convenience function returns the radial kernel for weak-lensing-like. Given an unnormalized redshift distribution and an optional magnification bias function, it returns two arrays: `chi`, `w(chi)`, where `chi` is an array of radial distances in units of Mpc and `w(chi)` is the lensing shear kernel (or the magnification one if `mag_bias` is not `None`).

#### Parameters

- **cosmo** (*Cosmology*) – cosmology object used to transform redshifts into distances.
- **dndz** (*tuple of arrays*) – A tuple of arrays (`z`, `N(z)`) giving the redshift distribution of the objects. The units are arbitrary; `N(z)` will be normalized to unity.
- **mag\_bias** (*tuple of arrays, optional*) – A tuple of arrays (`z`, `s(z)`) giving the magnification bias as a function of redshift. If `None`, `s=0` will be assumed

**class** `pyccl.tracers.tSZTracer` (*cosmo, z\_max=6.0, n\_chi=1024*)

Bases: `pyccl.tracers.Tracer`

Specific `Tracer` associated with the thermal Sunyaev Zel'dovich Compton- $\gamma$  parameter. The radial kernel for this tracer is simply given by

$$W(\chi) = \frac{\sigma_T}{m_e c^2} \frac{1}{1+z},$$

where  $\sigma_T$  is the Thomson scattering cross section and  $m_e$  is the electron mass.

Any angular power spectra computed with this tracer, should use a three-dimensional power spectrum involving the electron pressure in physical (non-comoving) units of  $eV \text{ cm}^{-3}$ .

#### Parameters

- **cosmo** (*Cosmology*) – Cosmology object.
- **zmax** (*float*) – maximum redshift up to which we define the kernel.
- **n\_chi** (*float*) – number of intervals in the radial comoving distance on which we sample the kernel.

### 14.1.3 Module contents



## 15.1 Unreleased

### 15.1.1 Python library

- Added more developer documentation (#776).
- Added number counts integrals for clusters (#787)

### 15.1.2 C library

- 

## 15.2 v2.1.0 Changes

### 15.2.1 Python library

- Perturbation theory power spectra #734
- Generalized Tinker mass function to all SO mass definitions (#736)
- Deprecated old halo model (#736)
- Halo model power spectra #717
- Fixed bug in Duffy 2008 concentration-mass relation #717
- Added a “spline” integration method to carry out Limber integrals.
- Added a function for the angular diameter distance difference between two scale factors (#645)
- Extended implementation of halo profiles (#722).
- Improved FFTLog API (#722).

- Functionality to resample 1D arrays including extrapolation (#720).
- Methods to retrieve internal tracer functions (#713).
- Improved implementation of halo model quantities (n(M), b(M), c(M)) (#668, #655, #656, #657, #636).
- Add straightforward single massive neutrino option (#730).
- Updated MG support via  $\mu / \Sigma$  (scale-independent) with higher accuracy implementation (#737)
- Added function to estimate the scale at which non-linear structure formation becomes important for the computation of the matter power spectrum (#760).

## 15.2.2 C library

- Deprecated old halo model (#736)
- Added a “spline” integration method to carry out Limber integrals.
- Added function for the angular diameter distance difference between two scale factors (#645)
- Removed old C/C++ examples (#725)
- Extended implementation of halo profiles (#722).
- Improved FFTLog API (#722).
- Functionality to resample 1D arrays including extrapolation (#720).
- Improved implementation of halo model quantities (n(M), b(M), c(M)) (#668, #655, #656, #657, #636).
- Updated MG support via  $\mu / \Sigma$  (scale-independent) with higher accuracy implementation (#737)

## 15.3 v2.0.1 Changes

### 15.3.1 Bug Fixes

- Fixed a PyPi installation bug where the proper files for CMAKE were not included in the source distribution.

## 15.4 v2.0 API changes

### 15.4.1 Python library

- Made CAMB the default Boltzmann code (#685).
- Added check to ensure the number of relativistic neutrinos is positive (#684).
- Added massive neutrinos to  $\Omega_m$  (#680).
- Changed neutrino API options to be intuitive and consistent (#681).
- Enabled CAMB (#677)
- Fixed bug when normalizing the linear power spectrum using  $\sigma_8$  and the  $\mu$ - $\Sigma$  modified gravity model (#677).
- Enabled the  $\mu$ - $\Sigma$  modified gravity model for any linear power spectrum (#677).

- Refactored the power spectrum normalization routines to only run CAMB/CLASS once when using sigma8 (#677).
- Fixed a bug where the power spectrum normalization was not being set accurately when using sigma8 (#677).
- Added warnings for inconsistent models (#676).
- Moved CLASS interface to python (#652).
- Moved all benchmarks and tests to python (#653).
- Changed IA bias normalization to be consistent with  $A_{IA}=1$  (#630).
- Implemented generalized models for tracers (#630)
- Improved error reporting for `angular_cl` computations (#567).
- Deprecated the `pyccl.redshifts` module (#579).
- Remove global splines for RSD correlation functions. These are now stored per cosmology. Further, they are now rebuilt on-the-fly for a given cosmology if a new scale factor is requested. (#582)
- Allow spline, numerical and constant parameters to be set from Python (#557).
- Deprecated transfer function options 'ccl\_emulator', 'ccl\_fitting\_function' 'ccl\_boltzmann', 'ccl\_boltzmann\_class' and 'ccl\_boltzmann\_camb' (#610). These were either not implemented or aliases for another option.
- Renamed transfer function option 'ccl\_none' to 'ccl\_transfer\_none' to avoid ambiguity (#610).
- Refactored transfer function and matter power spectrum options to allow any combination, even unphysical ones (#610).
- Added capability to use the halo model power spectrum as the primary non-linear power spectrum in the code (#610).
- Fixed infinite loop bug in splitting sum of neutrino masses into individual masses (#605).
- Added custom Halofit code (#611).
- Added `has_density` and `has_shear` tags to `Tracer` constructors.
- Changed TCMB to T\_CMB everywhere (#615)
- Deprecate Angpow (#571)
- Added support for modified gravity via  $\mu / \Sigma$  (scale-independent) parameterisation (#442)

## 15.4.2 C library

- Added massive neutrinos to `Omega_m` (#680).
- Moved CLASS interface to python (#652).
- Added OpenMP (#651).
- Removed all benchmarks from C and kept only the C unit tests in C (#653).
- Implemented generalized models for tracers (#630)
- Fixed memory leak in CLASS power spectrum computations (#561, #562).
- Fixed a bug where CLASS would crash due to small rounding errors at  $z = 0$  when evaluating power spectra (#563, #564).
- Fixed bug in `fftlog` for some complex arguments (#565, #566).

- Replaced custom gamma function with that from GSL (#570).
- Deprecated the `ccl_redshifts.h` functions (#579).
- Refactored spline and numerical parameters to be allocated per cosmology (#557).
- Allow global physical constants to be changed (#557).
- Fixed memory leaks in `ccl_correlation.c` (#581).
- Deprecated transfer function options ‘`ccl_emulator`’, ‘`ccl_fitting_function`’, ‘`ccl_boltzmann`’, ‘`ccl_boltzmann_class`’ and ‘`ccl_boltzmann_camb`’ (#610). These were either not implemented or aliases for another option.
- Renamed transfer function option ‘`ccl_none`’ to ‘`ccl_transfer_none`’ to avoid ambiguity (#610).
- Refactored transfer function and matter power spectrum options to allow any combination, even unphysical ones (#610).
- Added additional header and source files for clarity (#610).
- Added capability to use the halo model power spectrum as the primary non-linear power spectrum in the code (#610).
- Fixed infinite loop bug in splitting sum of neutrino masses into individual masses (#605).
- Added custom Halofit code (#611).
- Separated Limber and Non-Limber `C_ell` calculations (#614)
- Added `has_density` and `has_shear` flags to `ClTracers` (#614)
- Simplified `C_ell` unit tests (#614)
- Changed TCMB to `T_CMB` everywhere (#615)
- Fixed a small bug in the `w_tophat` expression and increased precision (#607)
- Deprecated the use of GSL spline accelerators (#626)
- Deprecate `Angpow` (#571)
- Added support for modified gravity via  $\mu / \Sigma$  (scale-independent) parameterisation (#442)

## 15.5 v 1.0 API changes :

### 15.5.1 C library

- Deprecated the `native` non-Limber angular power spectrum method (#506).
- Renamed `ccl_lsst_specs.c` to `ccl_redshifts.c`, deprecated LSST-specific redshift distribution functionality, introduced user-defined true  $dNdz$  (changes in call signature of `ccl_dNdz_tomog`). (#528).

### 15.5.2 Python library

- Renamed `lsst_specs.py` to `redshifts.py`, deprecated LSST-specific redshift distribution functionality, introduced user-defined true  $dNdz$  (changes in call signature of `dNdz_tomog`). (#528).
- Deprecated the `native` non-Limber angular power spectrum method (#506).
- Deprecated the `Parameters` object in favor of only the `Cosmology` object (#493).
- Renamed the `ClTracer` family of objects (#496).



- Various function parameter name changes and documentation improvements (#464).

## 15.6 v 0.4 API changes:

Summary: added halo model matter power spectrum calculation and halo mass-concentration relations. Change to  $\sigma(R)$  function so that it now has time dependence: it is now  $\sigma(R,a)$ . Added a  $\sigma_V(R,a)$  function, where  $\sigma_V(R,a)$  is the variance in the displacement field smoothed on scale  $R$  at scale-factor  $a$ .

### 15.6.1 C library

In `ccl_halomod.c`:

Added this source file. Contains functions to compute halo-model matter power spectra and also mass-concentration relations.

In `ccl_power.c`

Added  $\sigma_V$ , changed  $\sigma(R)$  ->  $\sigma(R,a)$

In `ccl_massfunc.c`

Added Sheth & Tormen (1999) mass function.

### 15.6.2 Python library

$\sigma_R(R)$  defaults to  $\sigma_R(R,a=1)$  unless  $a$  is specified.  $\sigma_V(R)$  is also added. New functions `ccl.halomodel_matter_power` and `ccl.halo_concentration`.

## 15.7 v 0.3 API changes:

Summary: the user interface for setting up cosmologies with neutrinos has been altered. Users should from now on pass  $N_{\text{eff}}$ , the effective number of relativistic neutrino species in the early universe, and  $m_{\text{nu}}$ , either a sum or neutrino masses or a set of 3 neutrino masses.

### 15.7.1 C library

In `ccl_core.c`:

In the function, `ccl_parameters_create`, the arguments `double N_nu_rel`, and `double N_nu_mass` have been removed. The arguments `double Neff` and `ccl_mnu_convention mnu_type` have been added. The argument `mnu` has changed in type from `double mnu` to `double* mnu`.

Similar changes apply in `ccl_cosmology_create_with_params` and all `ccl_parameters_create...nu` convenience functions.

Additionally, in the function `ccl_parameters_create` and `ccl_cosmology_create_with_params`, arguments have been added for the parameters of the BCM baryon model; these are `double bcm_log10Mc`, `double bcm_etab`, and `double bcm_ks`.

In `ccl_neutrinos.c`:

The function `ccl_Omeganh2_to_Mnu` has been renamed `ccl_nu_masses`. The arguments `double a` and `gsl_interp_accel* accel` have been removed. The argument `ccl_neutrino_mass_splits mass_split` has been added.

## 15.7.2 Python wrapper

In `core.py`:

In the `Parameters` class, the arguments `'N_nu_rel'`, and `'N_nu_mass'` have been removed. The optional arguments `'Neff'`, `'mnu_type'`, `'bcm_log10Mc'`, `'bcm_etab'`, and `'bcm_ks'` have been added. Similar changes occur in the `Cosmology` class.

In `neutrinos.py`:

In the function `Omeganuh2`, the argument `'Neff'` has been removed. It is now fixed to the length of the argument `'mnu'`. The function `'Omeganuh2_to_Mnu'` has been renamed `'nu_masses'`. The arguments `'a'` and `'Neff'` have been removed. The argument `'mass_split'` has been added. The argument `'TCMB'` has been changed to `'T_CMB'`.

## 15.7.3 Other changes since release 0.2.1 (September 2017):

`CLASS` is no longer included as part of `CCL`; it can instead be easily downloaded via the `class_install.py` script and this procedure is documented.

Tutorial added for usage with `MCMC`

Added support for `BCM` baryon model

cpp compatibility improved

Python 3 support added

Added support for computing the nonlinear matter power spectrum with `CosmicEmu`

Added support for `CMB` lensing observables, including splines for cosmological quantities to higher redshift

Added the ability to return useful functions such as `dNdz` for a tracer `Cl` object.

Clarified license

Values of the physical constants have changed to `CODATA2014/IAU2015`

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